

# Visual Imaging and the Electronic Age

## *Color Science*

### *Grassman's Experiments & Trichromacy*

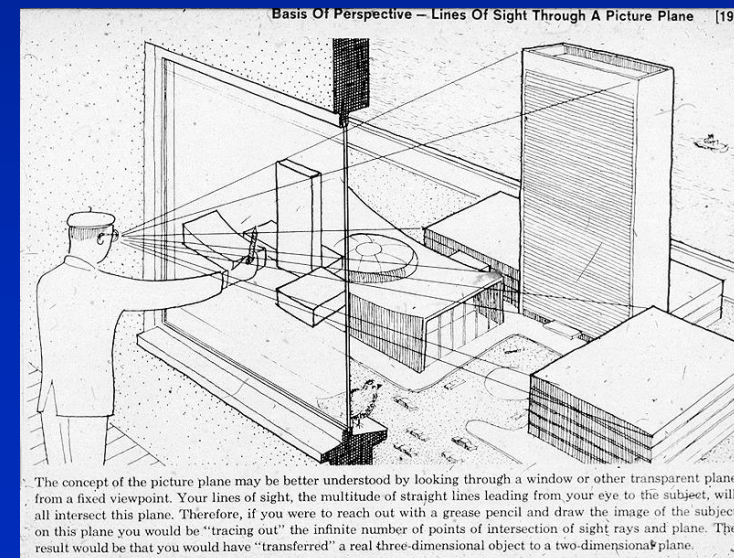
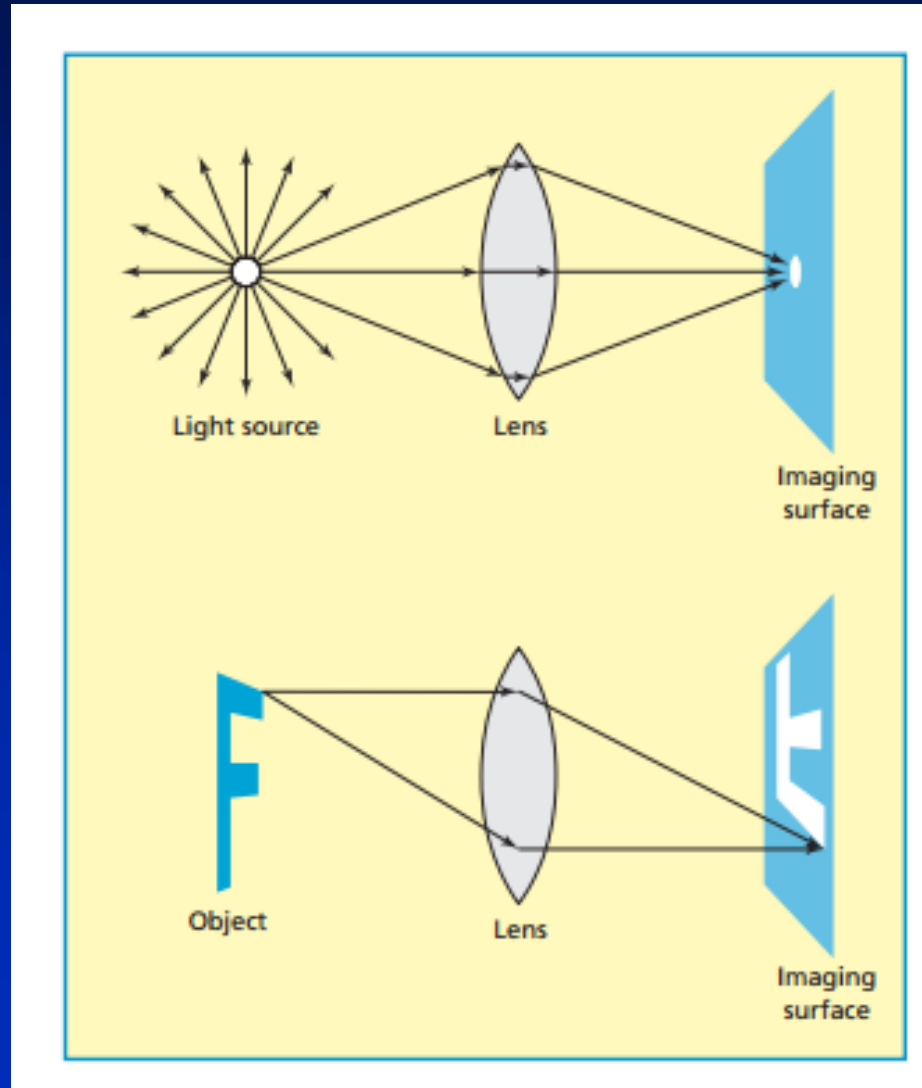
Lecture #5

September 17, 2020

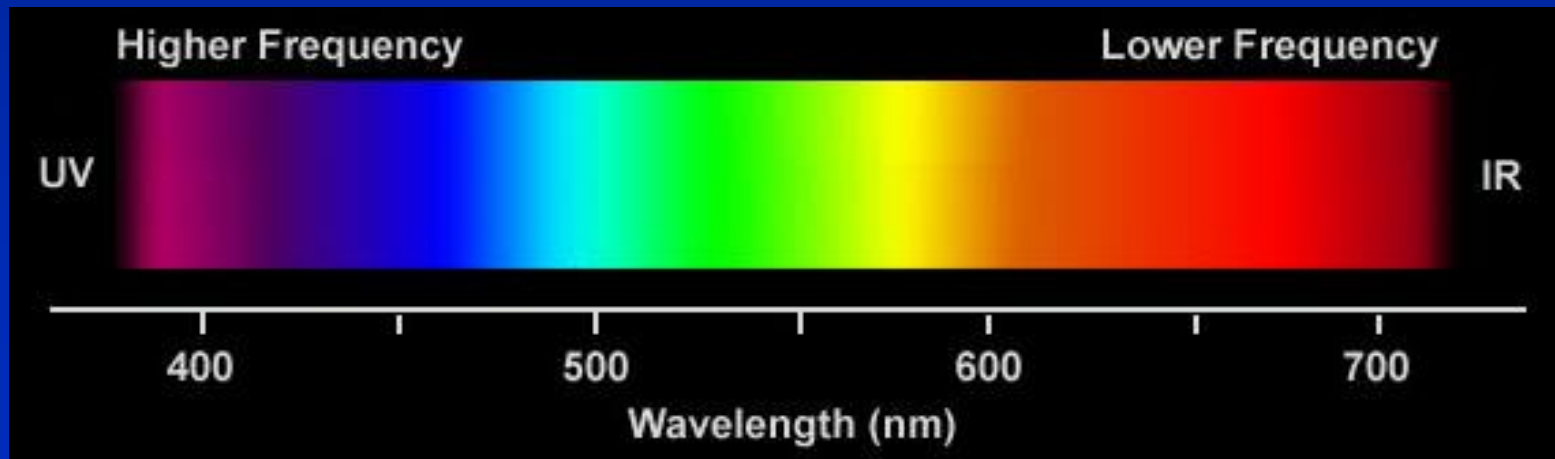
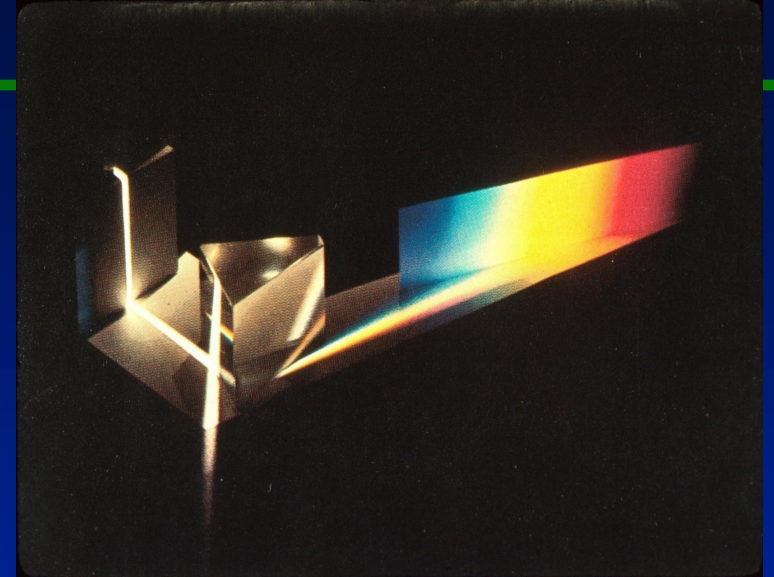
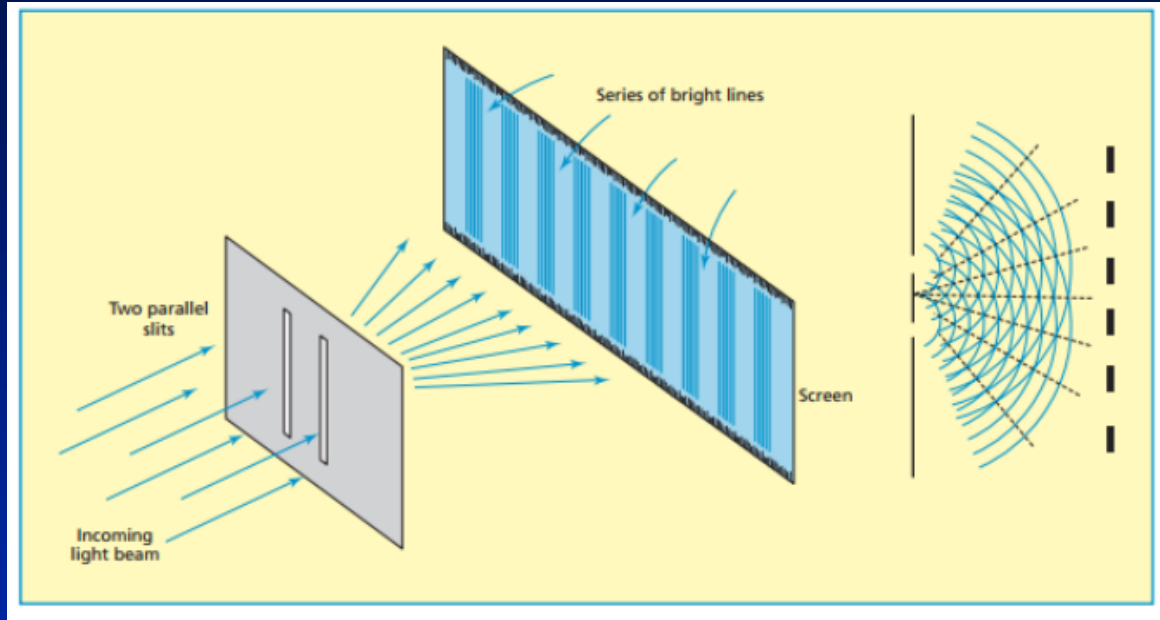
Prof. Donald P. Greenberg

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- Required Reading:
  - Roy S. Berns. "Principles of Color Technology," 2000 John Wiley & Sons, Inc., Chapter 1. PDF
  - None
  - References:
  
  - Foundations of Color Science Lecture.
  - S. Deleniv. "The Basic Neurobiology Behind the Recently Famous 12-Dot Illusion." September 17, 2016. The Neurosphere.
  - R.C. Dougal. "Maxwell's First Coloured Light Sources: Artists' Pigments," Colour in Art, Design and Nature, WIT Press, 2011
  - Holland Cotter. "Harmony, Harder than it Looks," The New York Times, July 27, 2012. The New York Times
  - Dr. R.W.G. Hunt. "The Reproduction of Colour," 1995, Fifth Edition, Fountain Press.
  - Gunter Wyszecki & W.S. Stiles. "Color Science," 1967 John Wiley & Sons, Inc.
  - Tom N. Cornsweet. "Visual Perception," 1970, Academic Press.

# Light as Rays

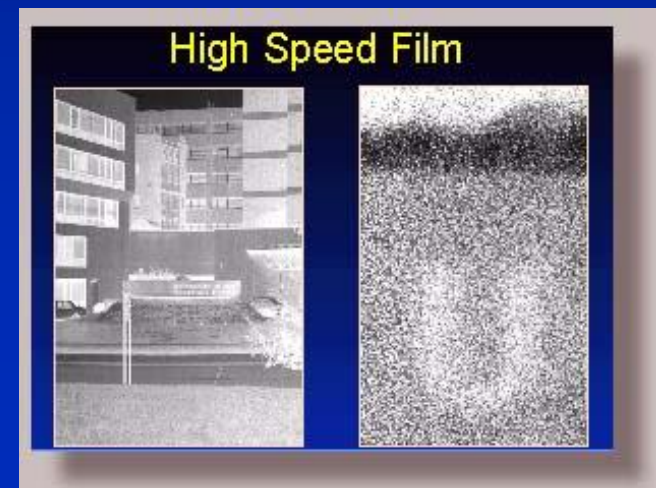
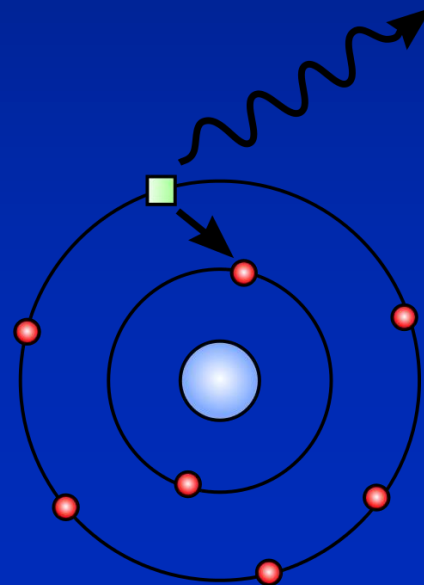
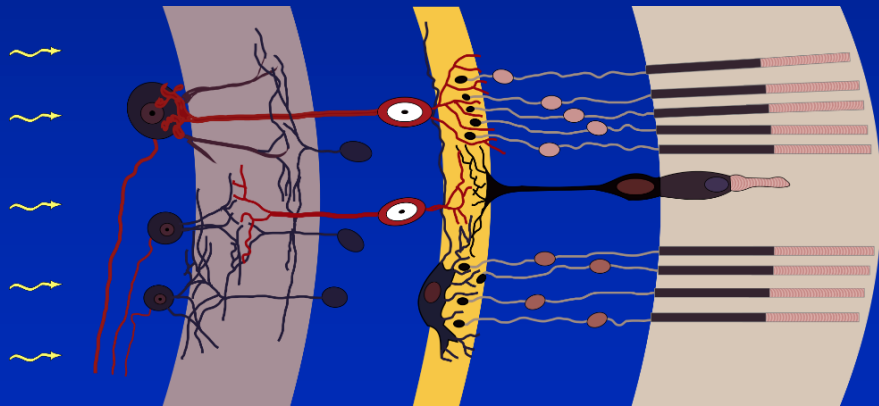
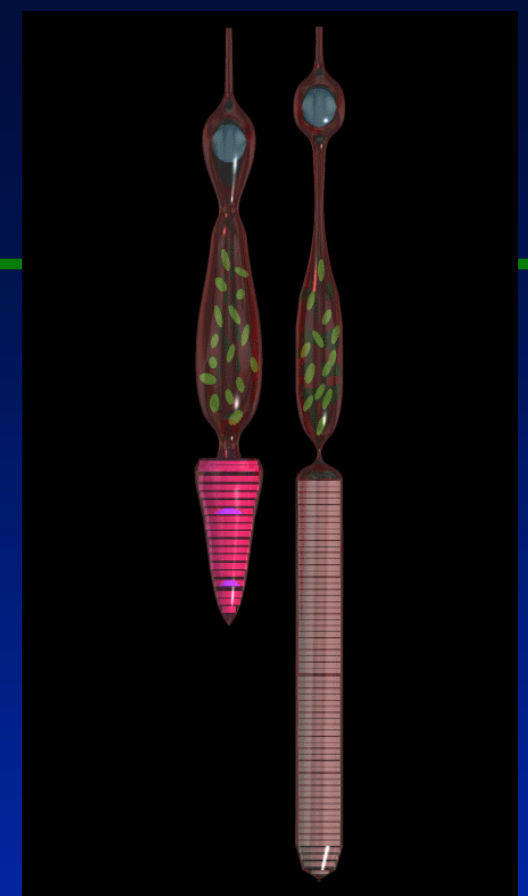
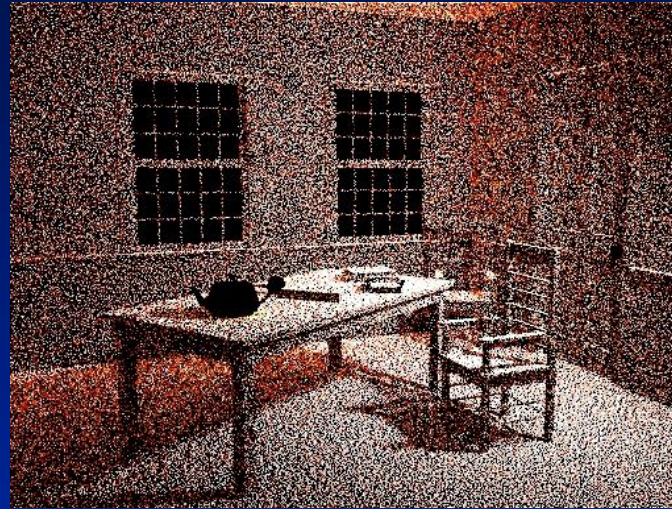
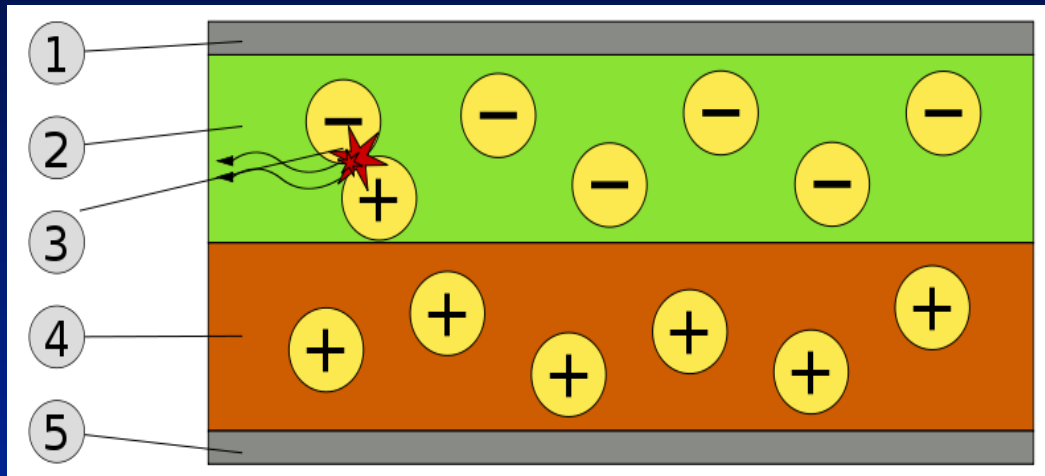


# Light as Waves



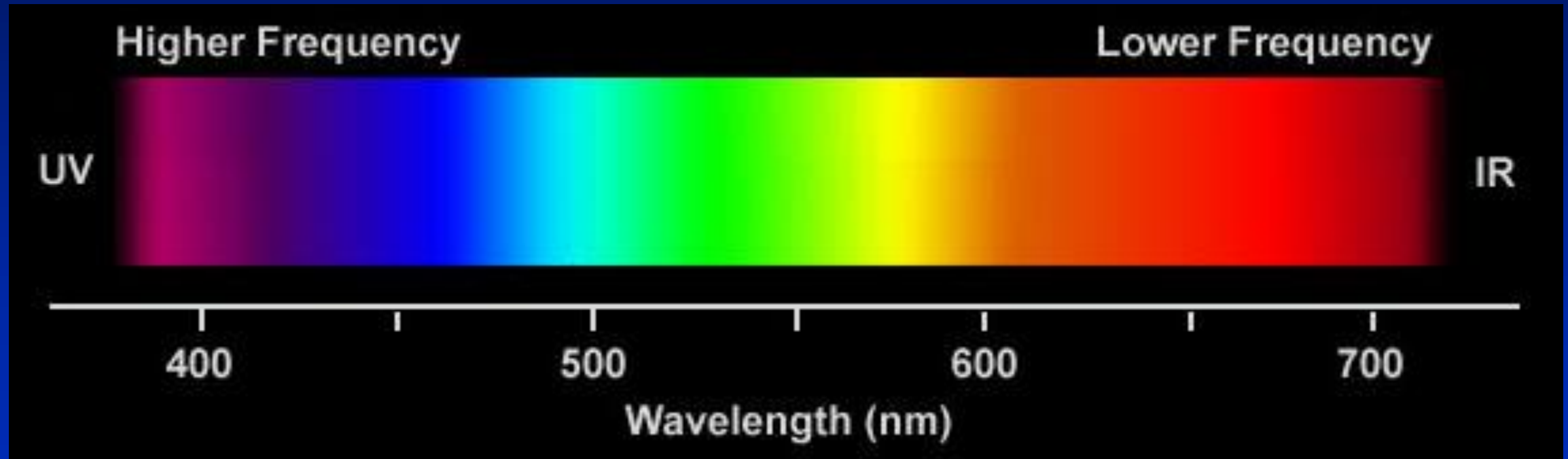


# Light as Photons

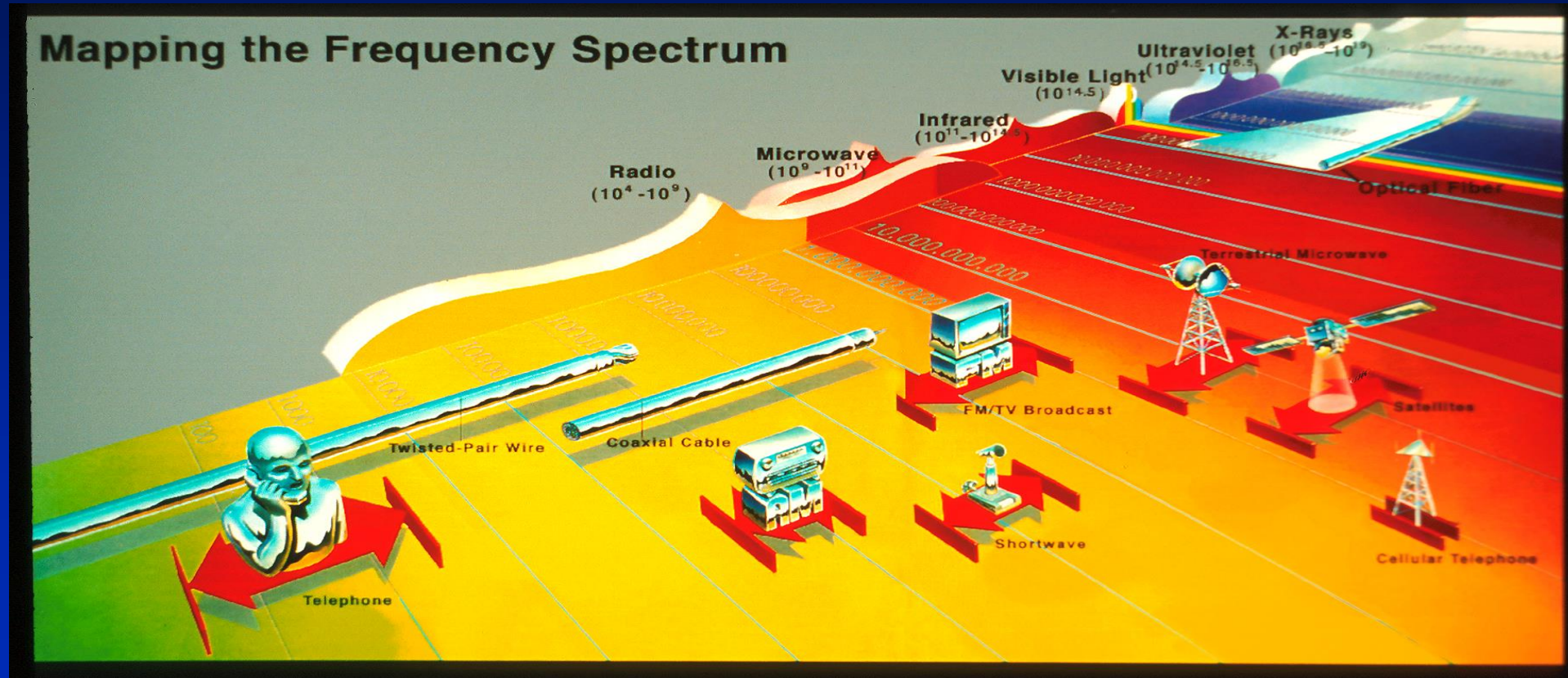


# Visible Light Spectrum

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# Frequency Spectrum





# What is Color Science?

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- Quantifying the physical energy which reaches the eye (physical)
- Determining the information which is sent from the retina (rods and cones) through the optic nerve to the human visual system (physiological stimuli)
- How does the brain interpret this information? (cognitive)



# What is Color Science?

---

- Quantifying the physical energy which reaches the eye (physical)
- Determining the information which is sent from the retina (rods and cones) through the optic nerve to the human visual system (physiological stimuli)
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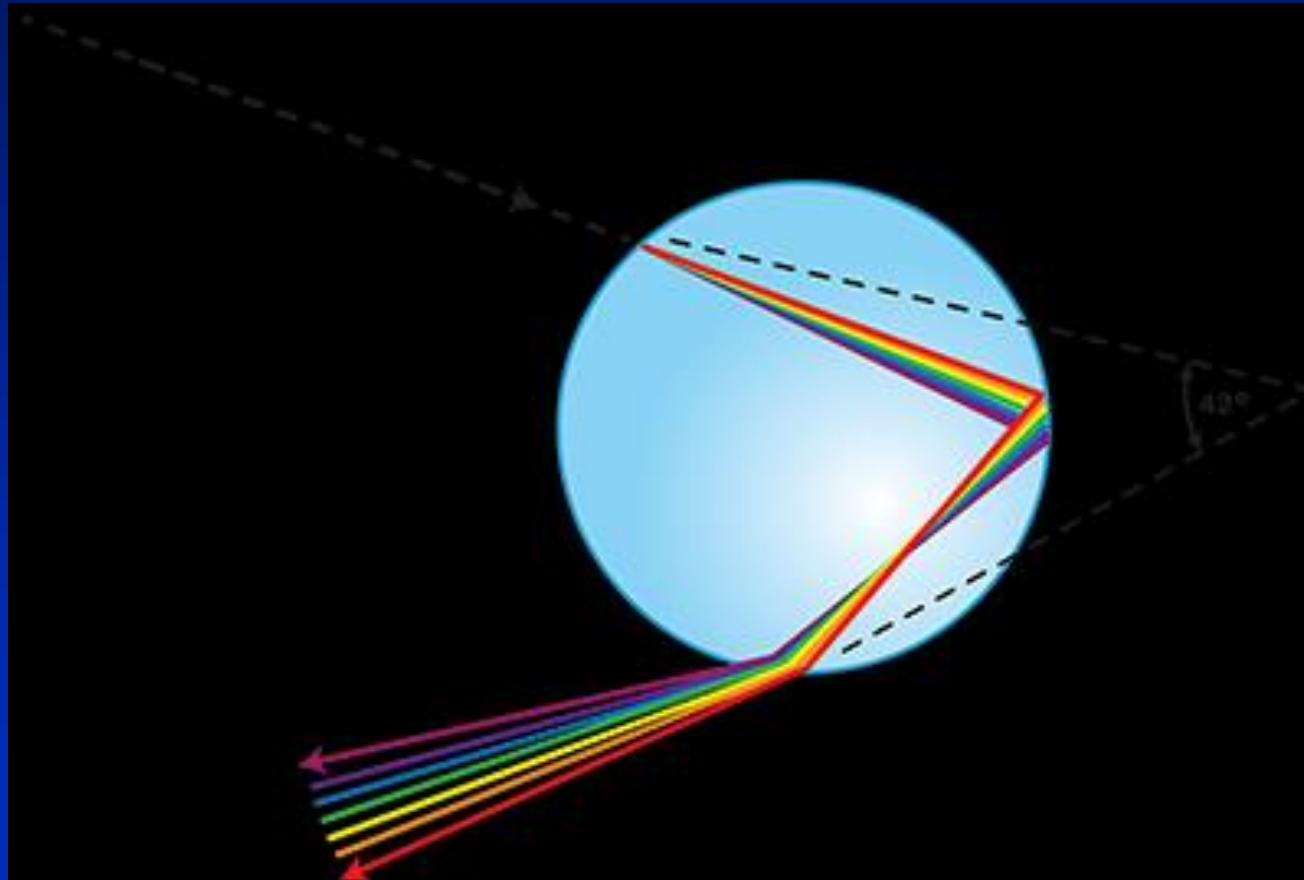
# Color

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Rainbow over London.

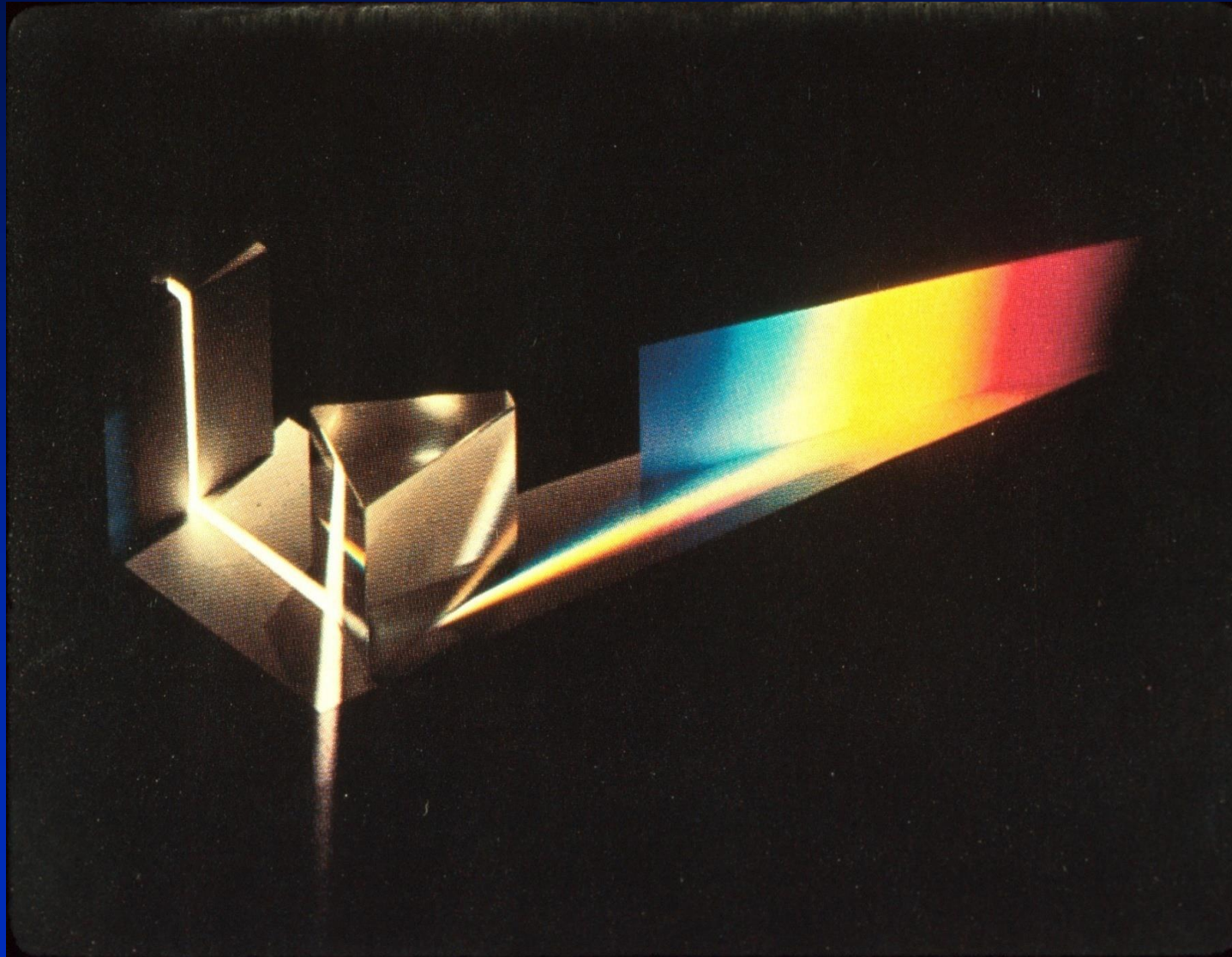
# What Causes the Colors of the Rainbow?



Water  
droplet

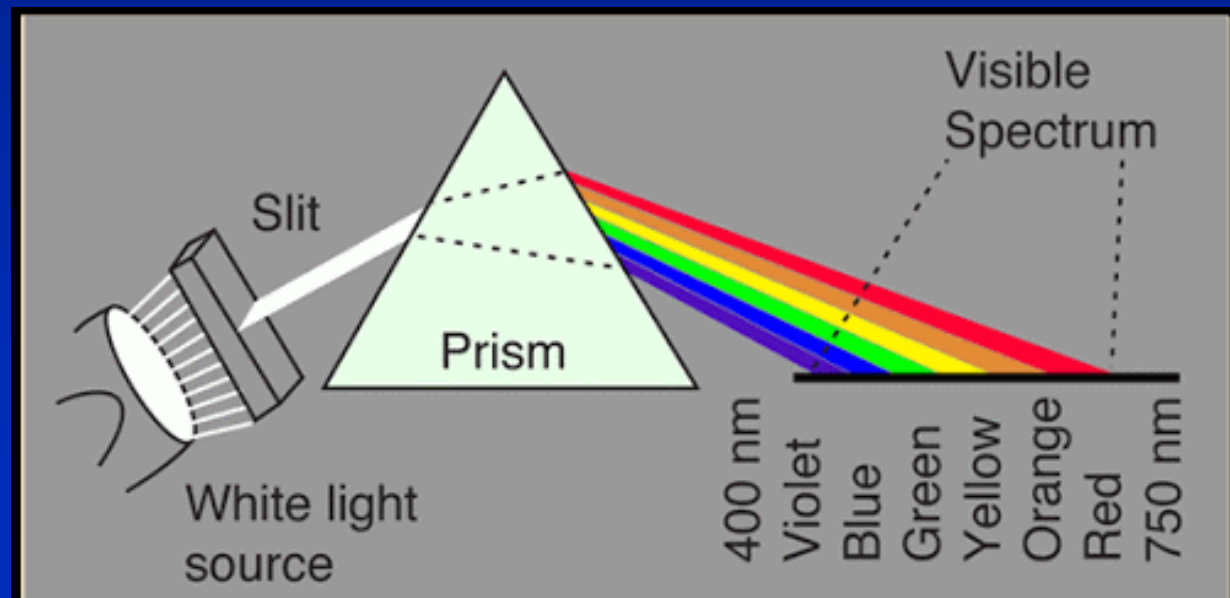
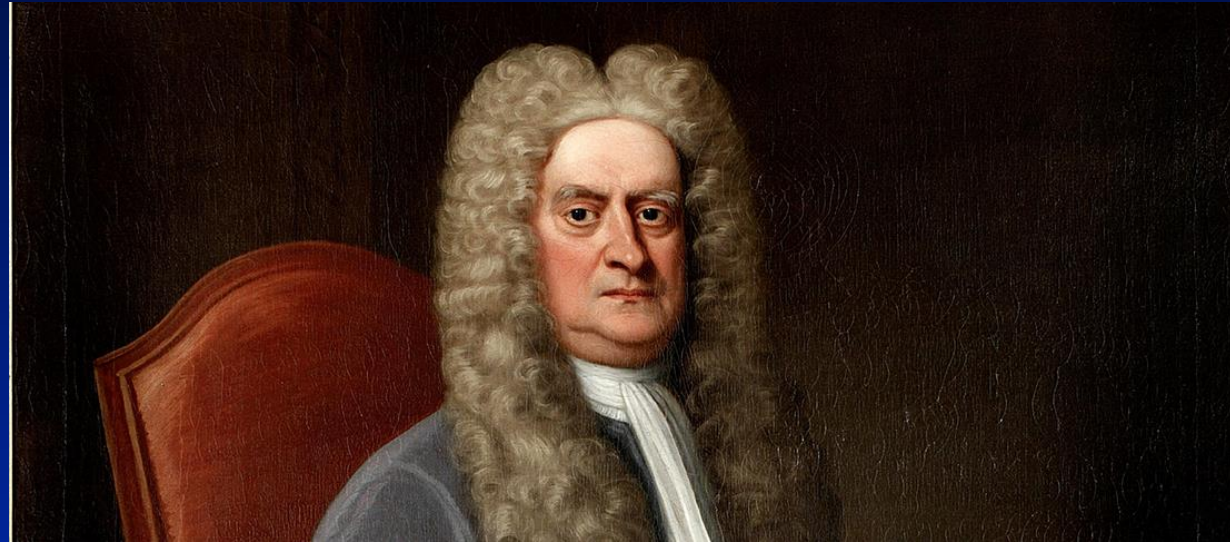
# Color

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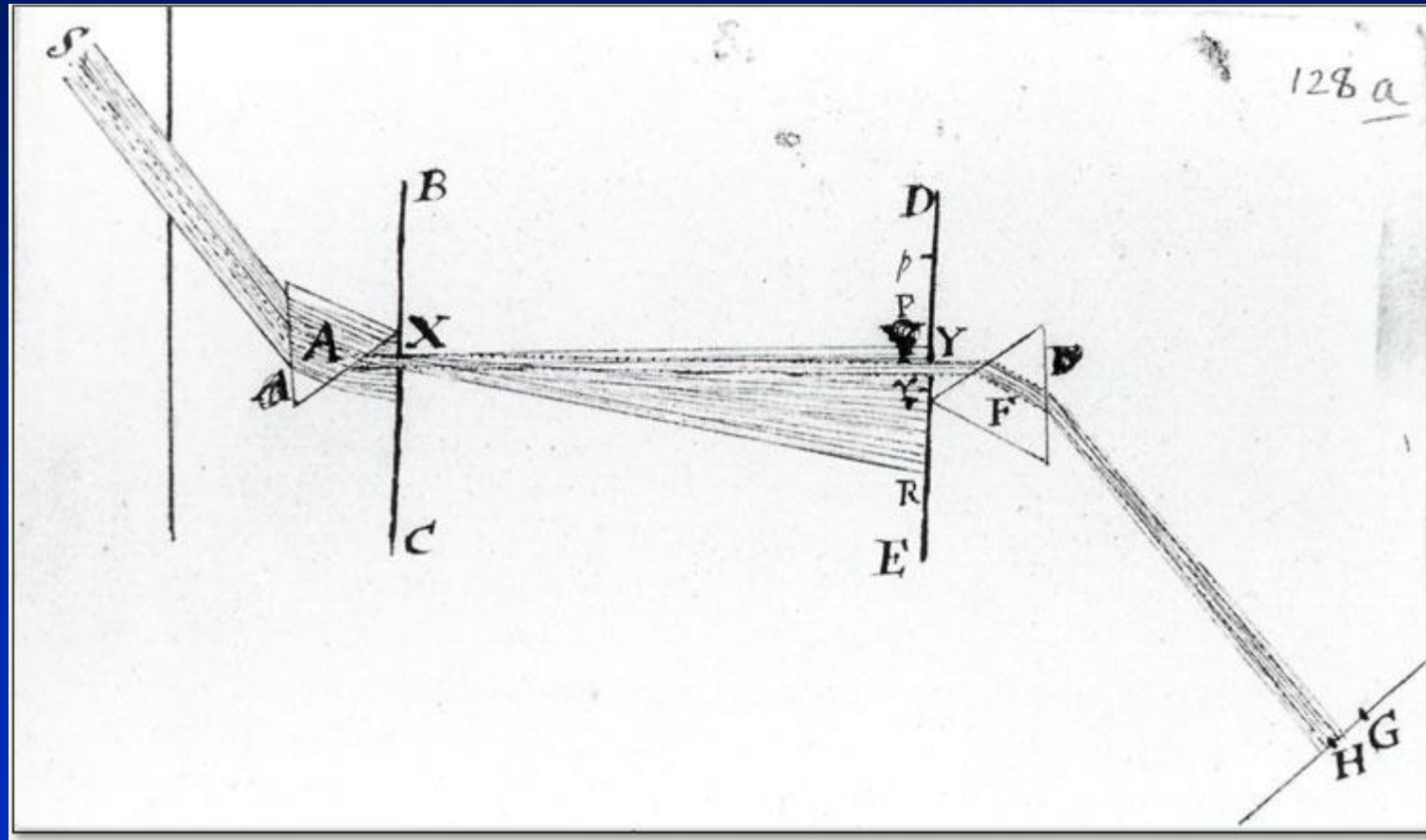


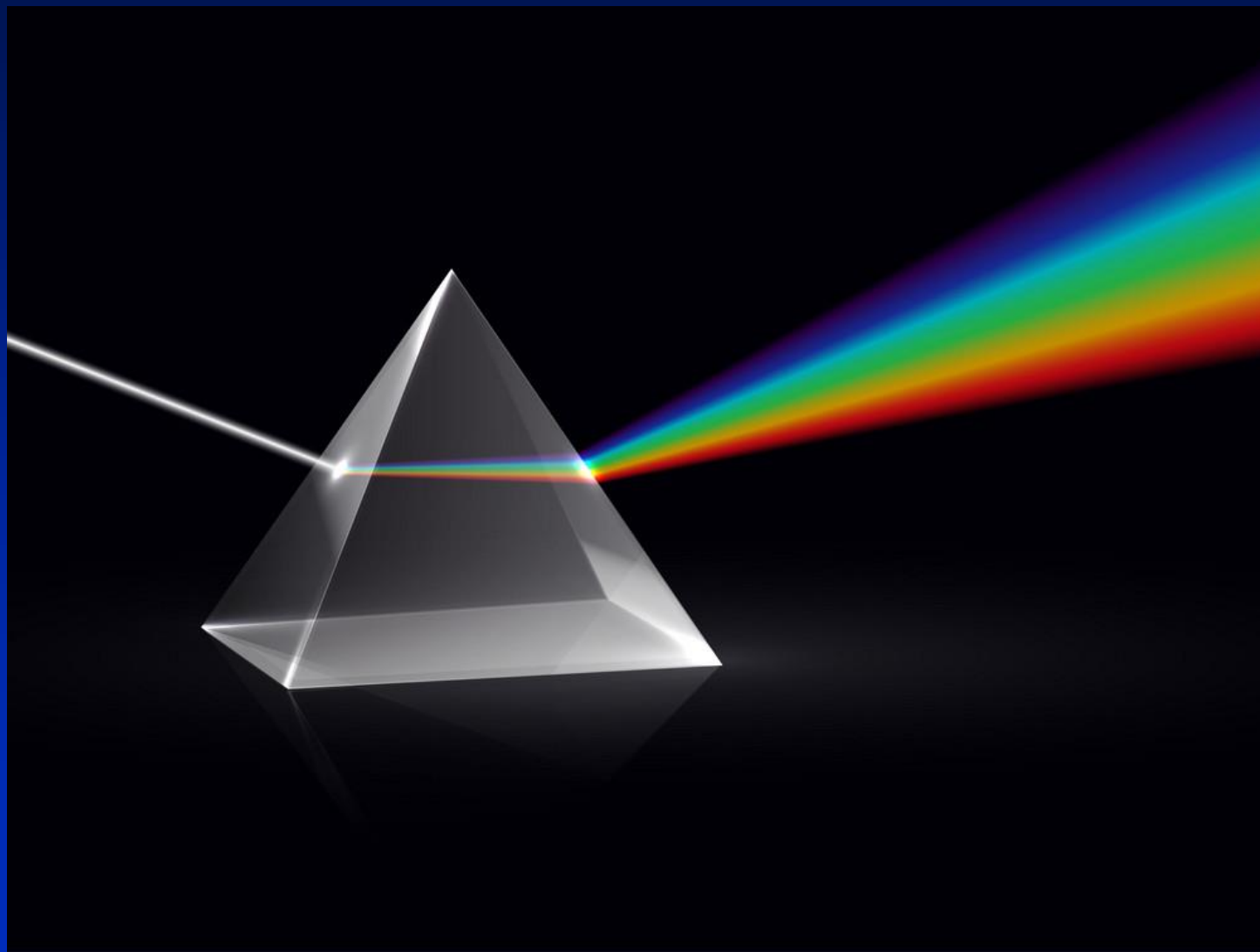
# Newton's Color Spectrum



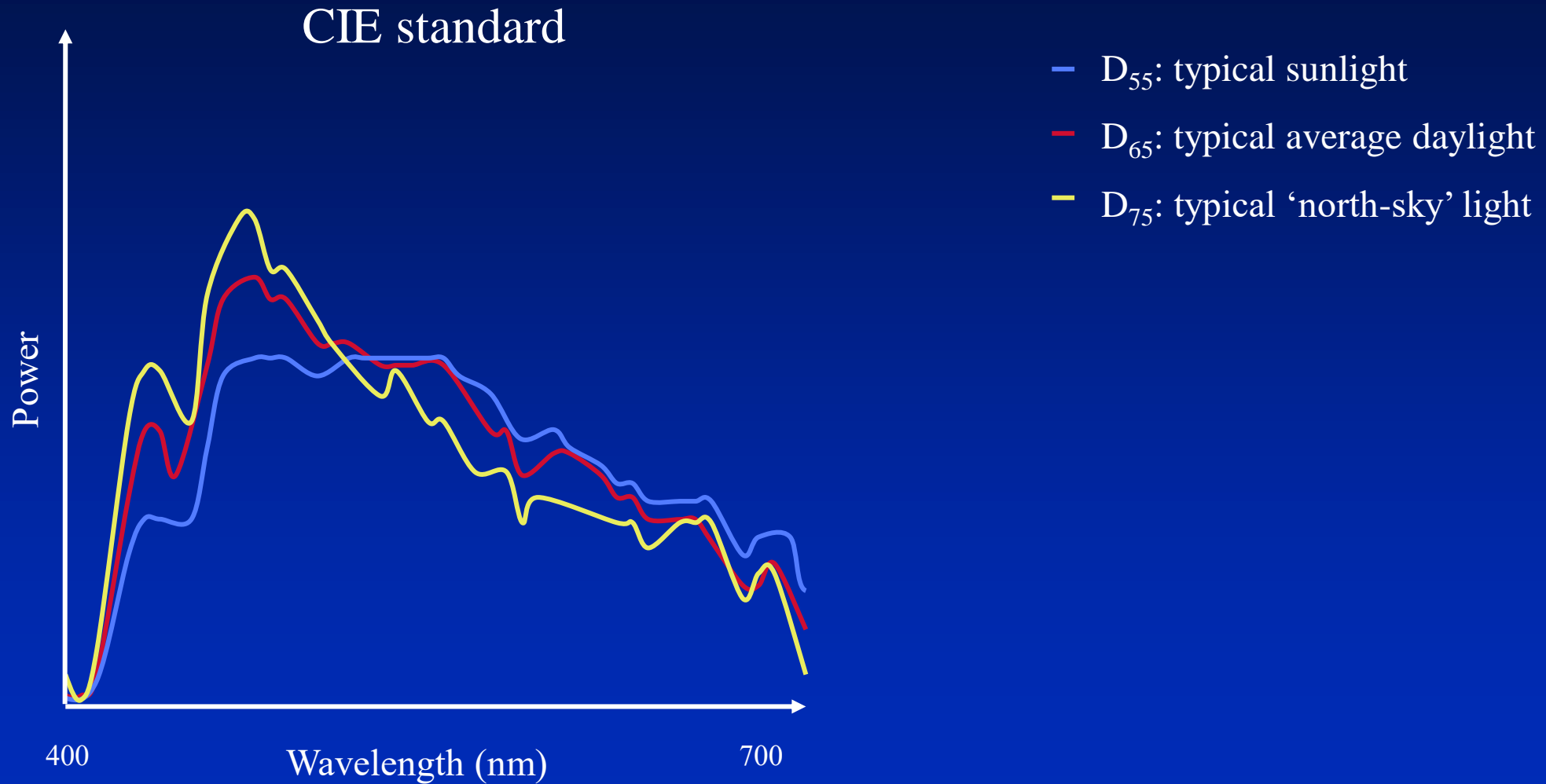
# Newton and the Color Spectrum

1672





# Spectral Distributions of Natural Outdoor Light Sources

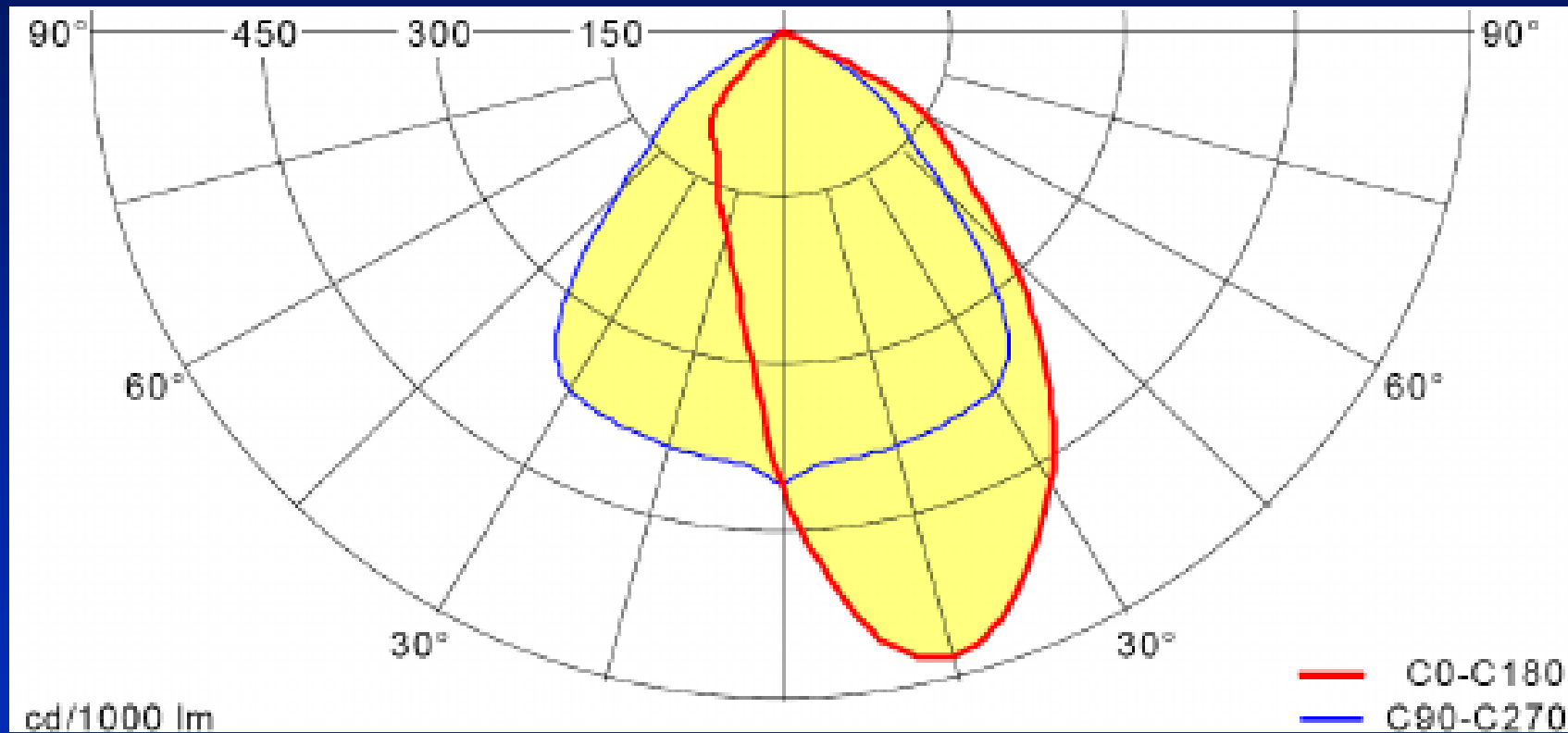






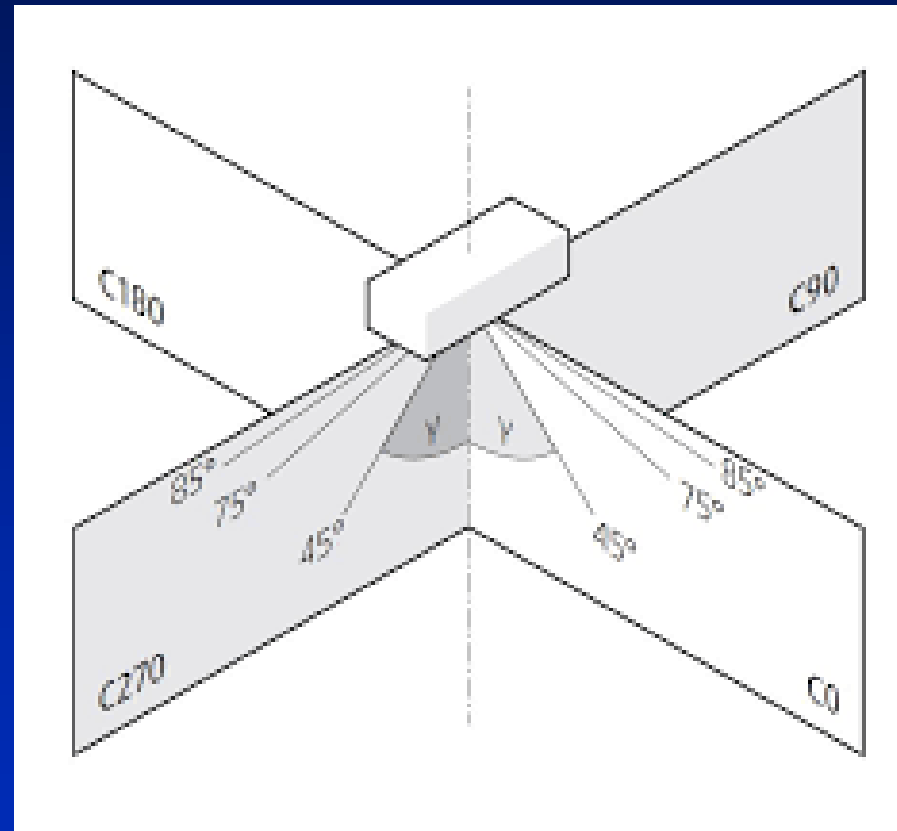
# Indoor Light Source

# Goniometric Diagram



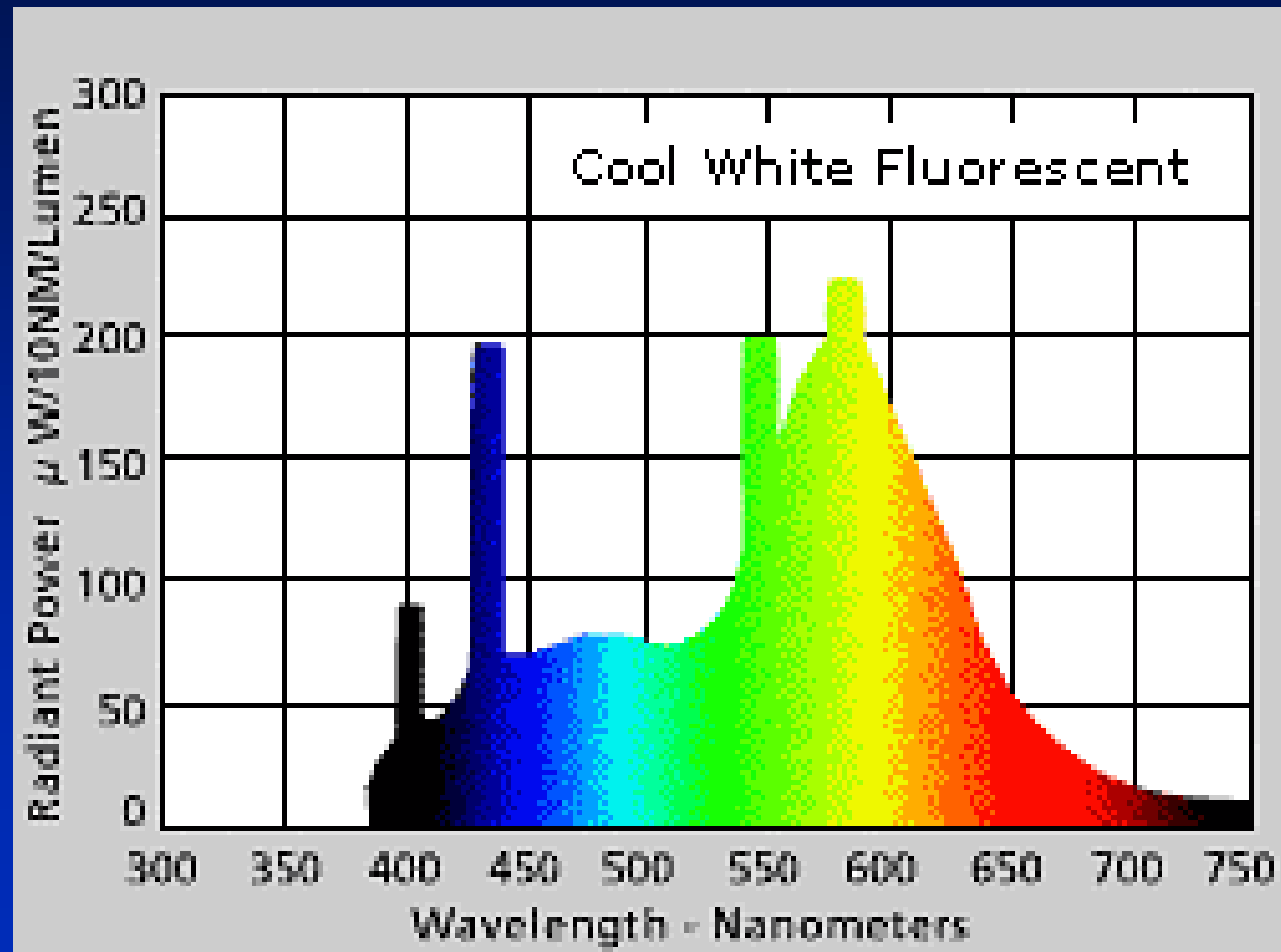
# Indoor Light Source

# Goniometric Diagram



# Spectral Distribution

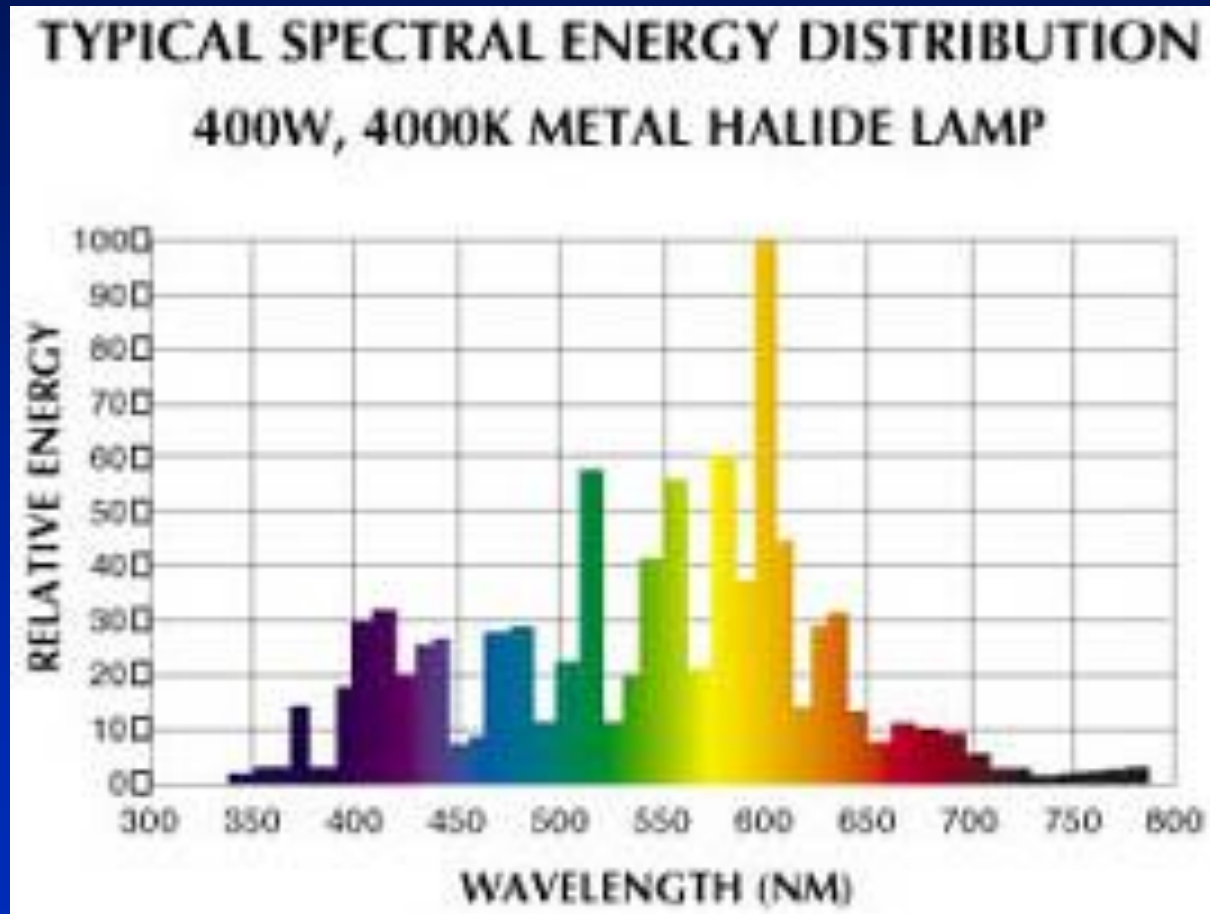
# Fluorescent Light





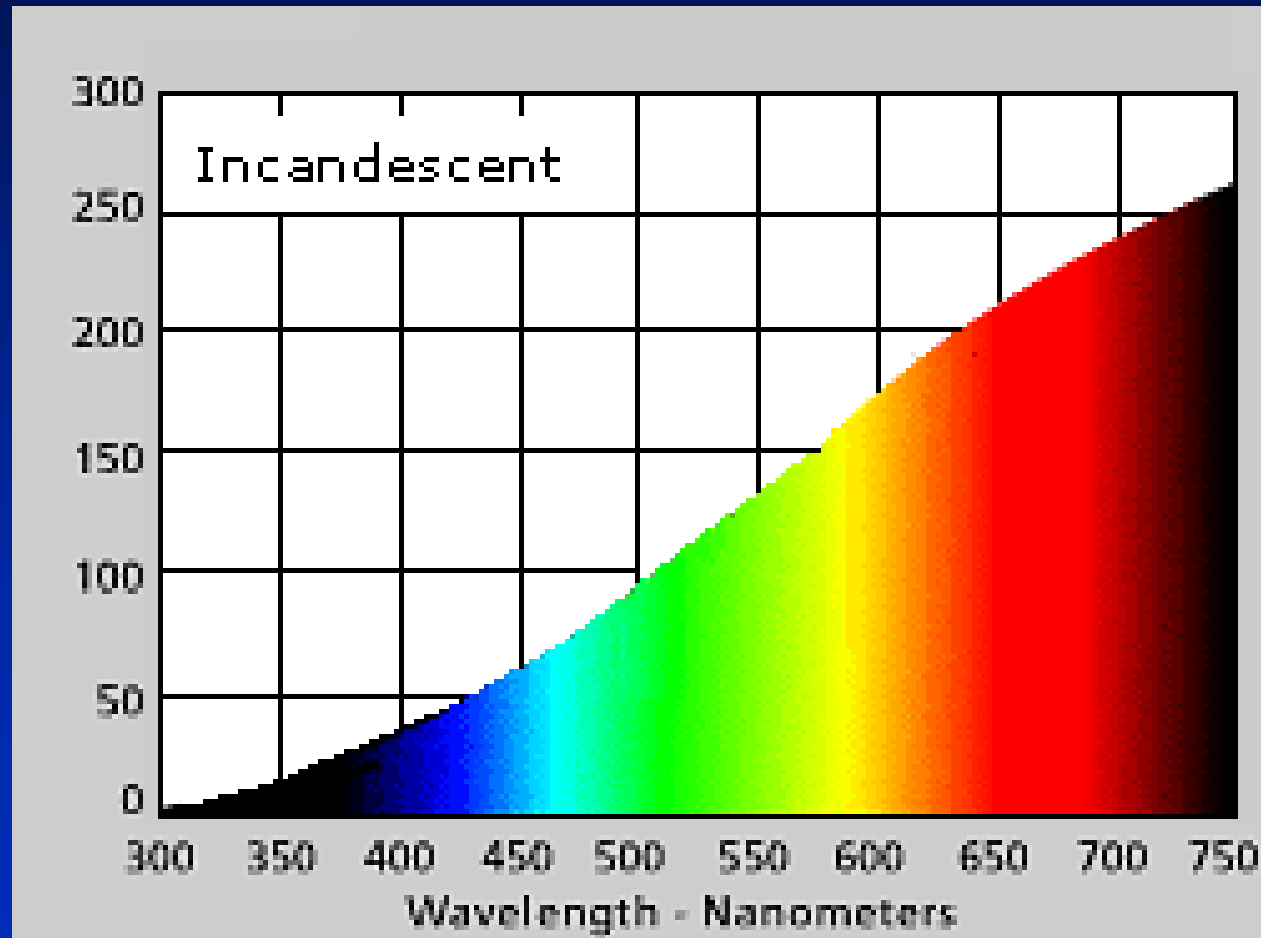
# Spectral Distribution

# Metal Halide Lamp



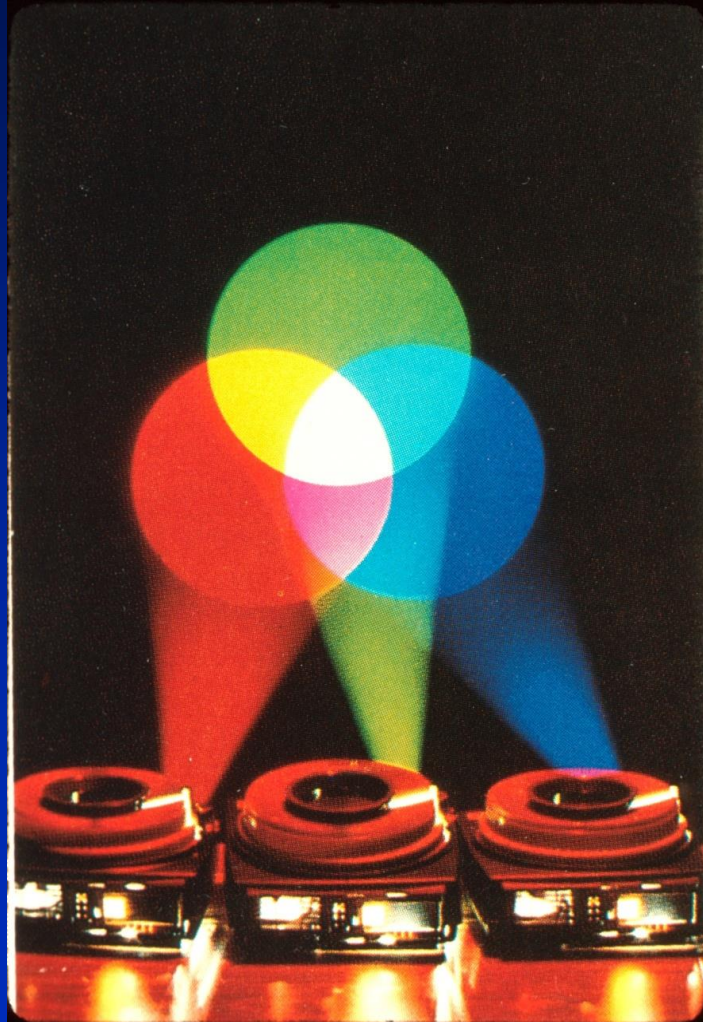
# Spectral Distribution

# Incandescent Light



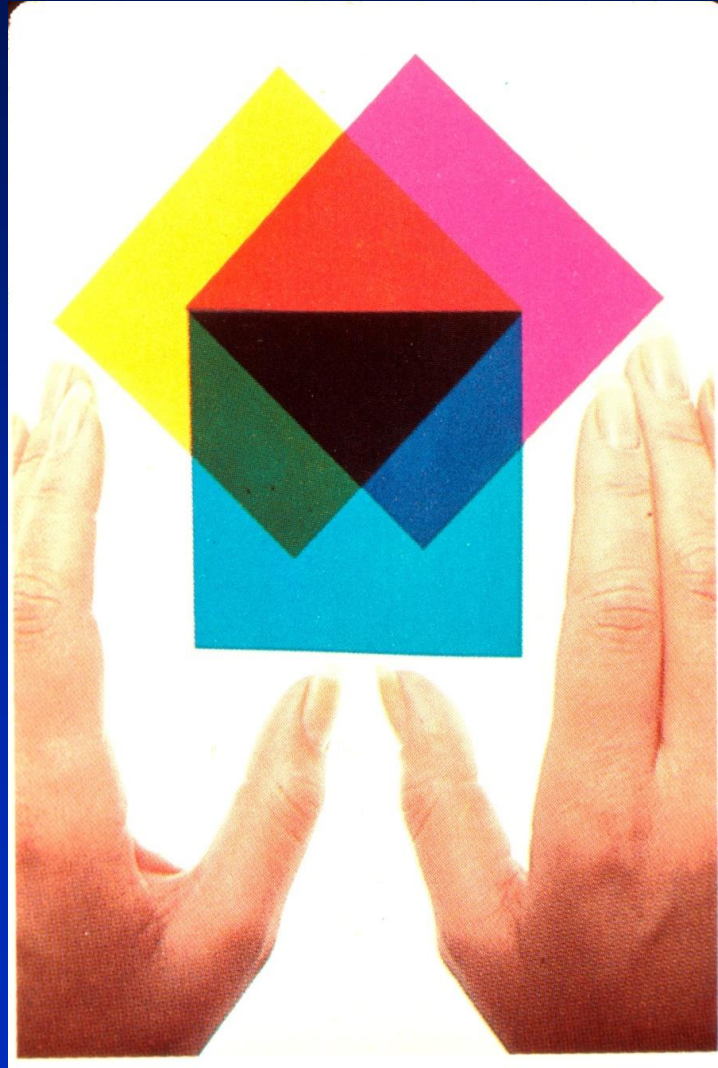
# Additive Color

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# Subtractive Color

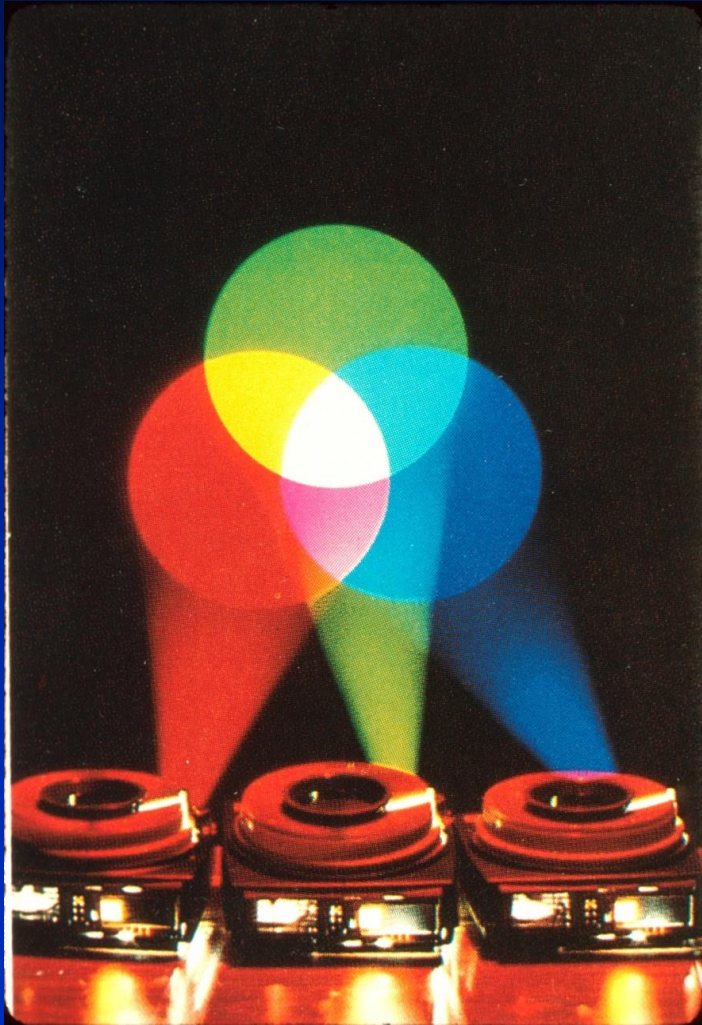
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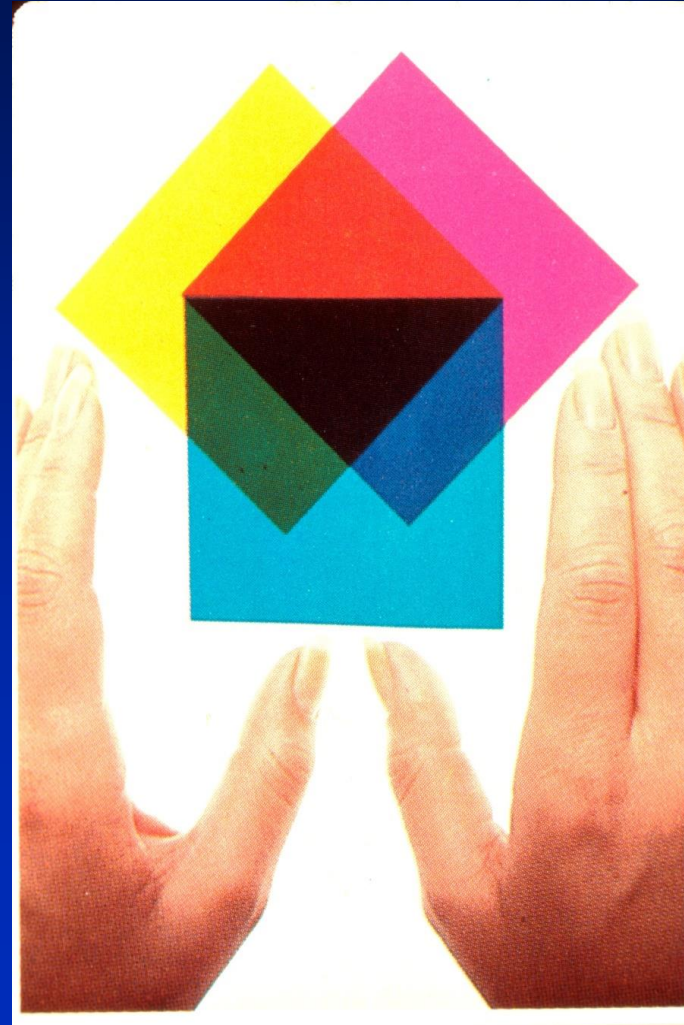


# Additive & Subtractive Color Spaces

RGB



CMY





# Printer Inks



Black

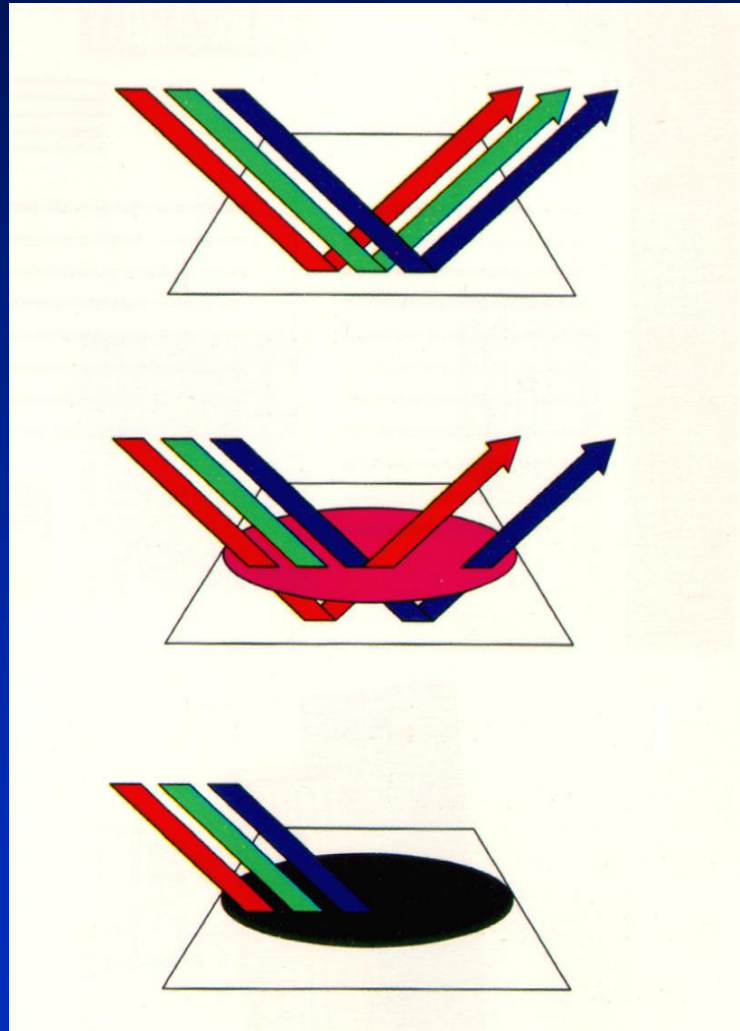
Cyan

Magenta

Yellow

# Subtractive Reflection Processes

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# Emitted Light

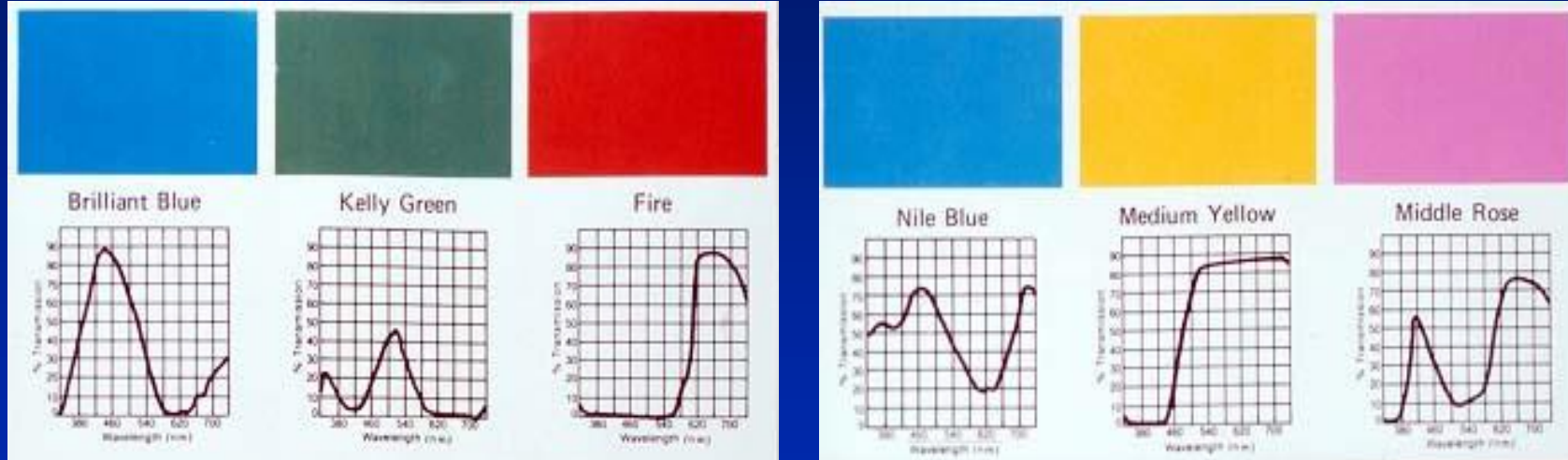
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$$P = \sum_{\lambda} E_{\lambda} \quad P = \int_{390}^{700} E_{\lambda} d\lambda$$

$P$  = energy reaching the eye at all wavelengths

$E_{\lambda}$  = emitted light energy at each wavelength

# Spectral Distributions of Reflective Colors



# Reflected Light

$$P = \sum_{\lambda} E_{\lambda} \quad (\text{Emitted Light})$$

$$P = \sum_{\lambda} E_{\lambda} \cdot \rho_{\lambda} \quad P = \int_{390}^{700} E_{\lambda} \cdot \rho \lambda d\lambda$$

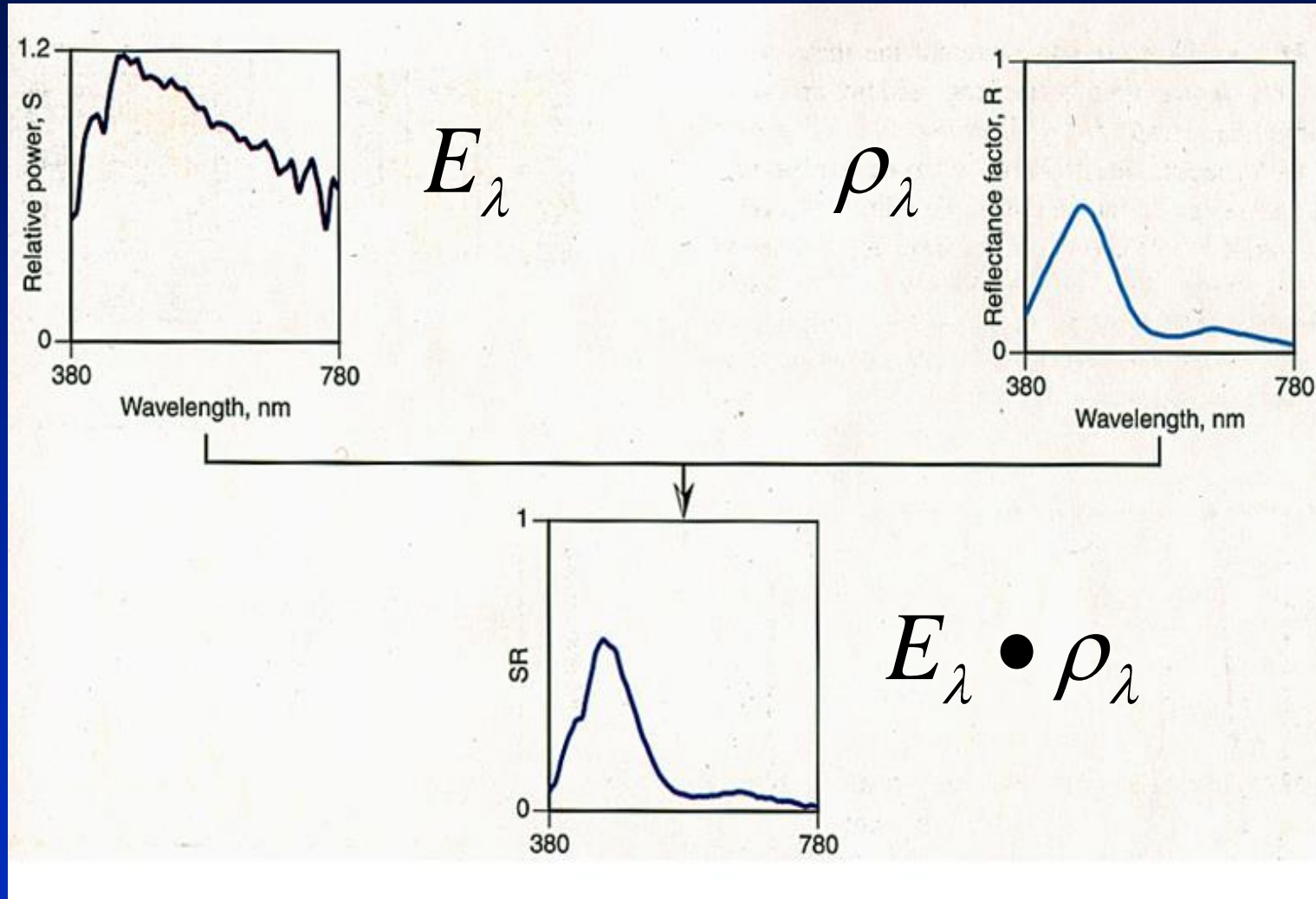
$P$  = energy reaching the eye at all wavelengths

$E_{\lambda}$  = emitted light energy at each wavelength

$\rho_{\lambda}$  = reflected light energy at each wavelength

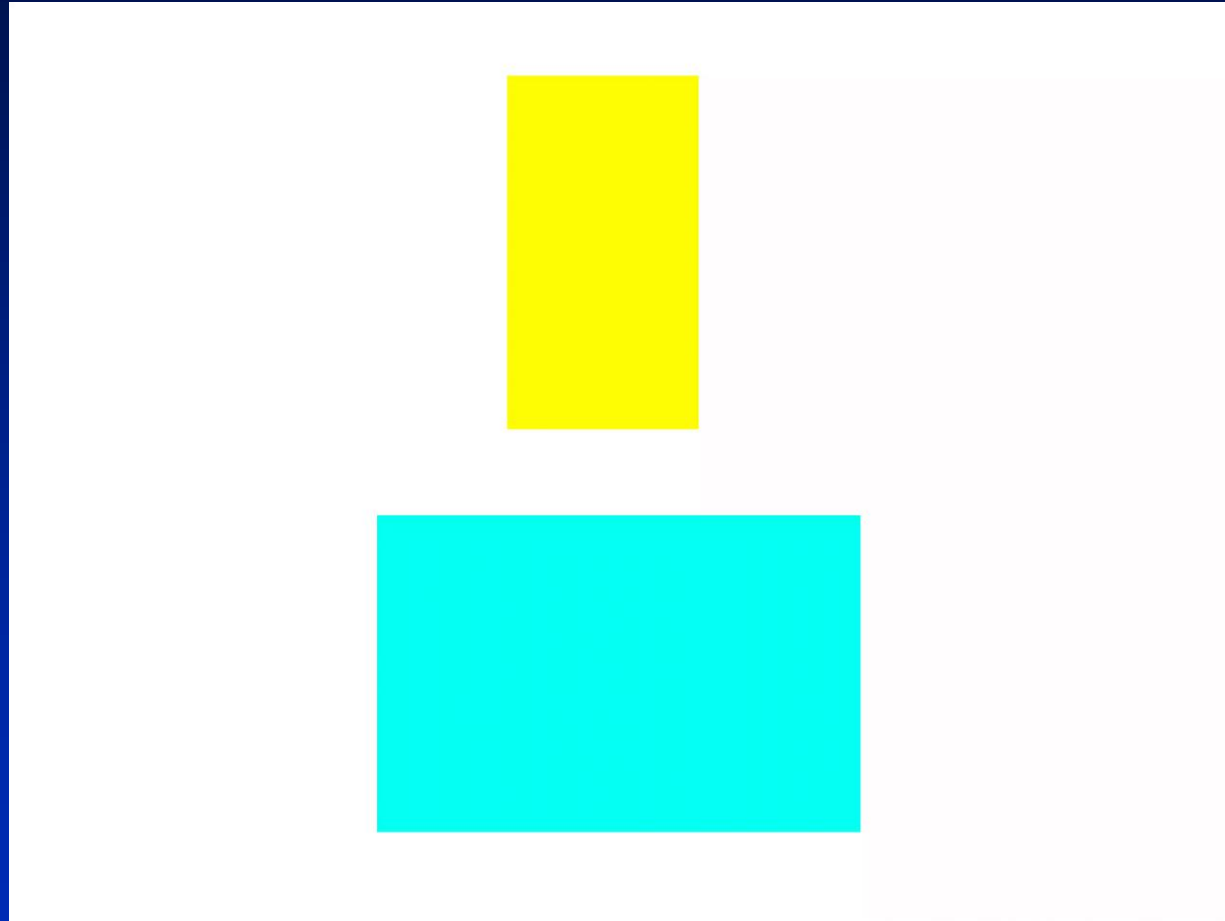


# Reflected Light



# Opaque Video

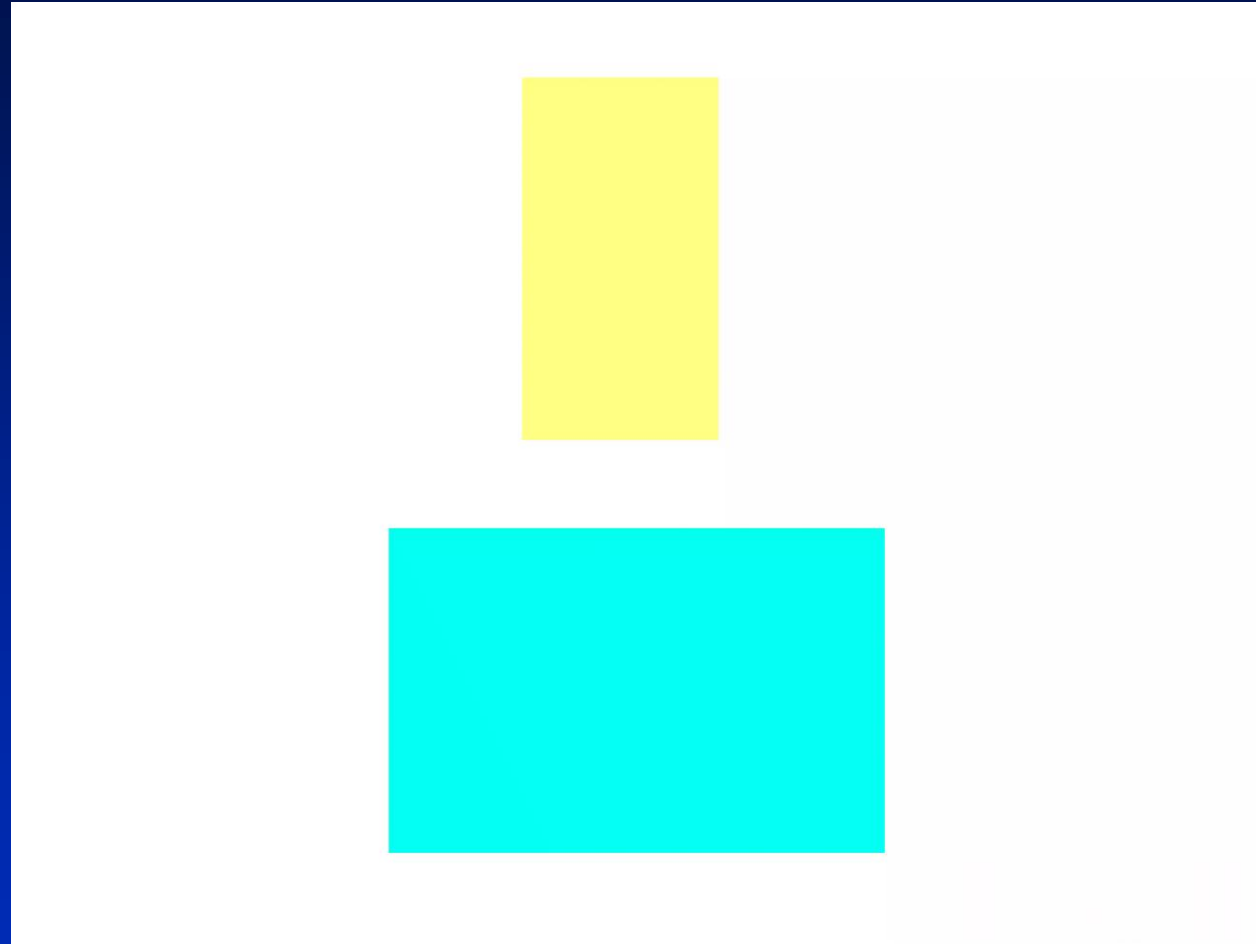
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$$\alpha_{yellow} = 1$$

$$C_o = \alpha_a \cdot C_a + (1 - \alpha_a) \cdot C_b$$

# Transparency Video



$$\alpha_{yellow} = 0.5$$

$$C_o = \alpha_a \cdot C_a + (1 - \alpha_a) \cdot C_b$$

# Transmitted Light

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$$P = \int_{390}^{700} E_{\lambda} \cdot d_{\lambda}$$

$$P = \int_{390}^{700} E_{\lambda} \cdot p_{\lambda} \cdot d_{\lambda}$$

$$P = \int_{390}^{700} E_{\lambda} \cdot t_{\lambda} \cdot d_{\lambda}$$

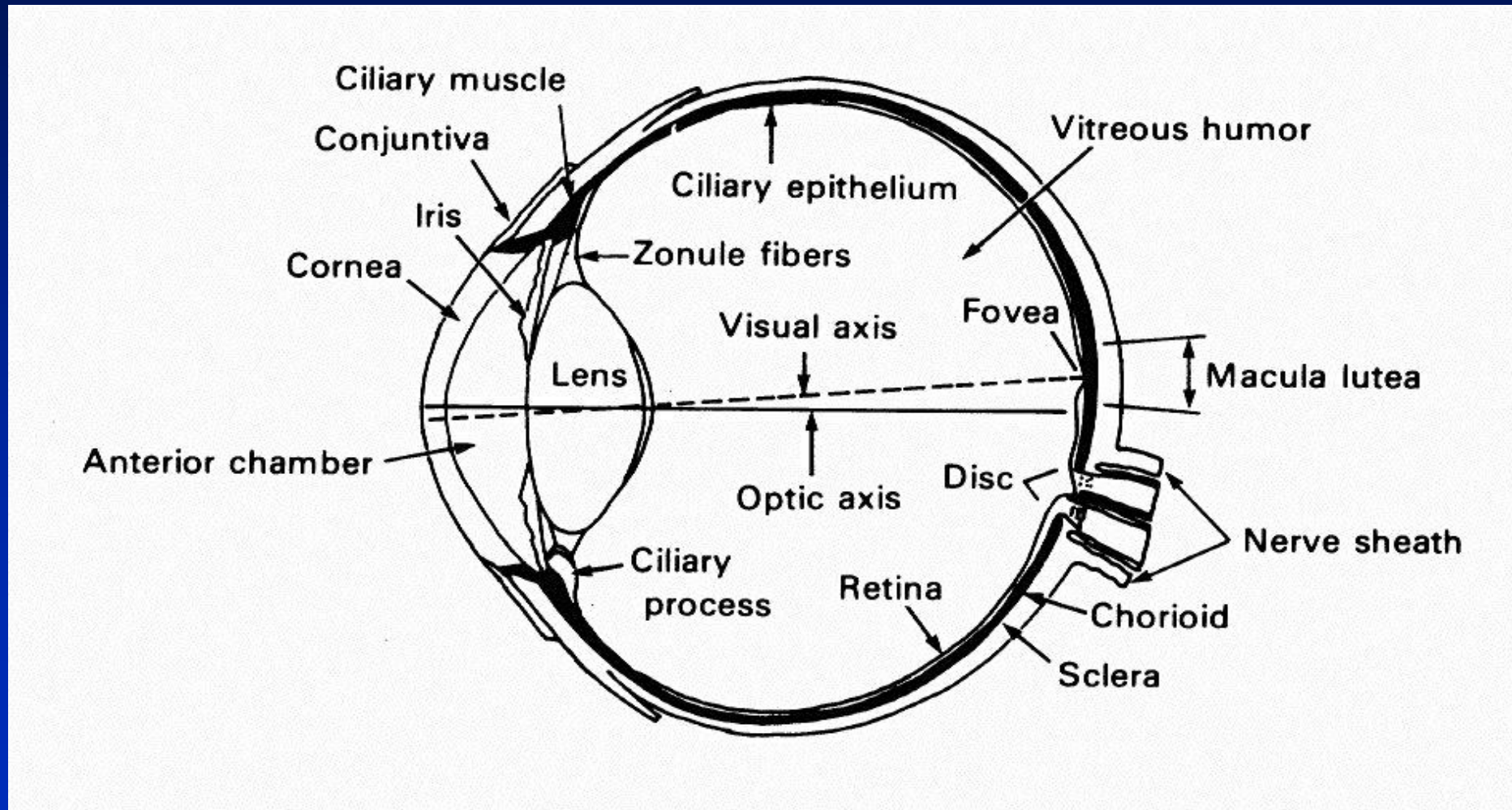
# What is Color Science?

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- Quantifying the physical energy which reaches the eye (physical)
- Determining the information which is sent from the retina (rods and cones) through the optic nerve to the human visual system (physiological stimuli)
- How does the brain interpret this information? (cognitive)



# Cross Section of Eye & Retina

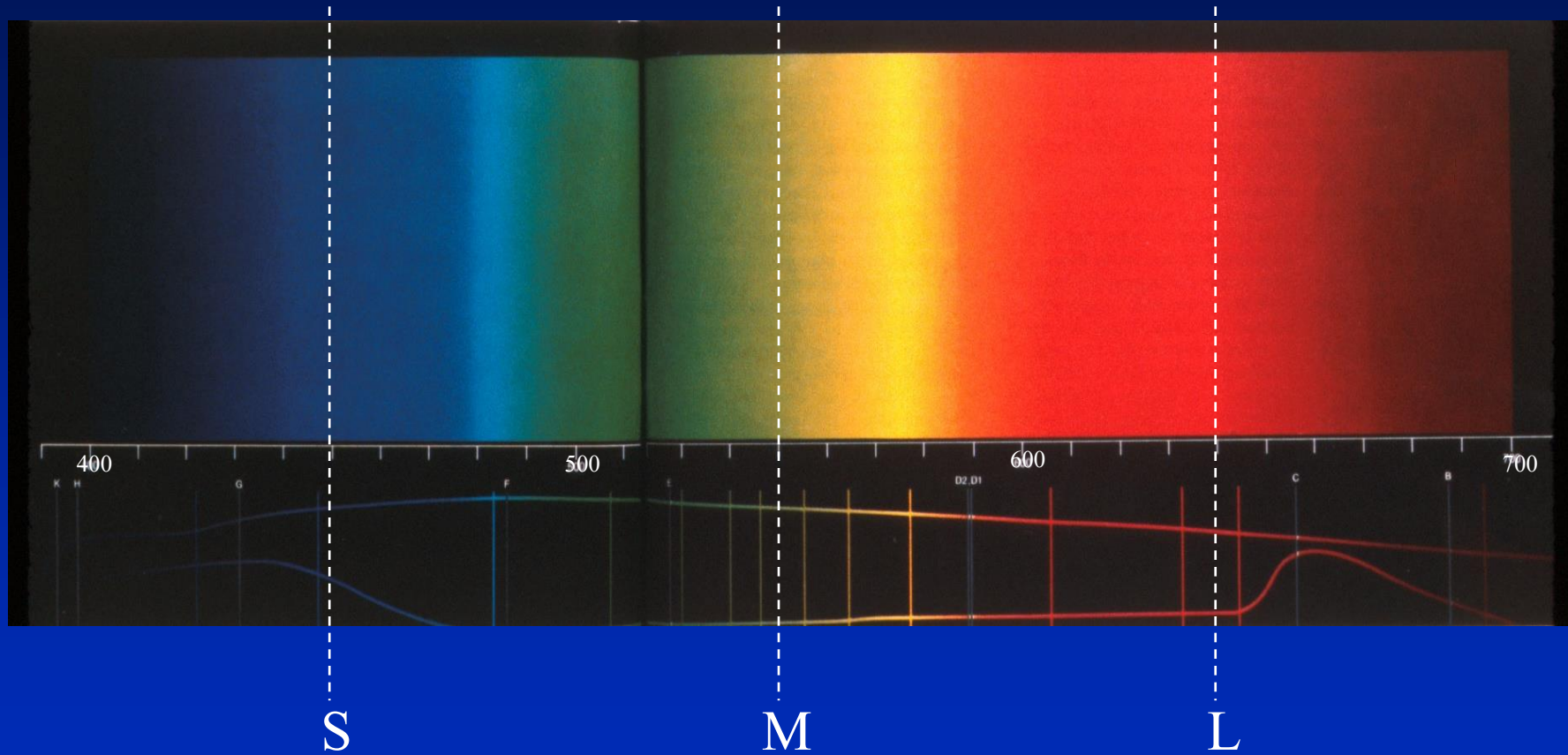


# Rods & Cones

Comparison of a rod cell (right) and cone cell (left). This shows how each cell acquired its name from its shape.



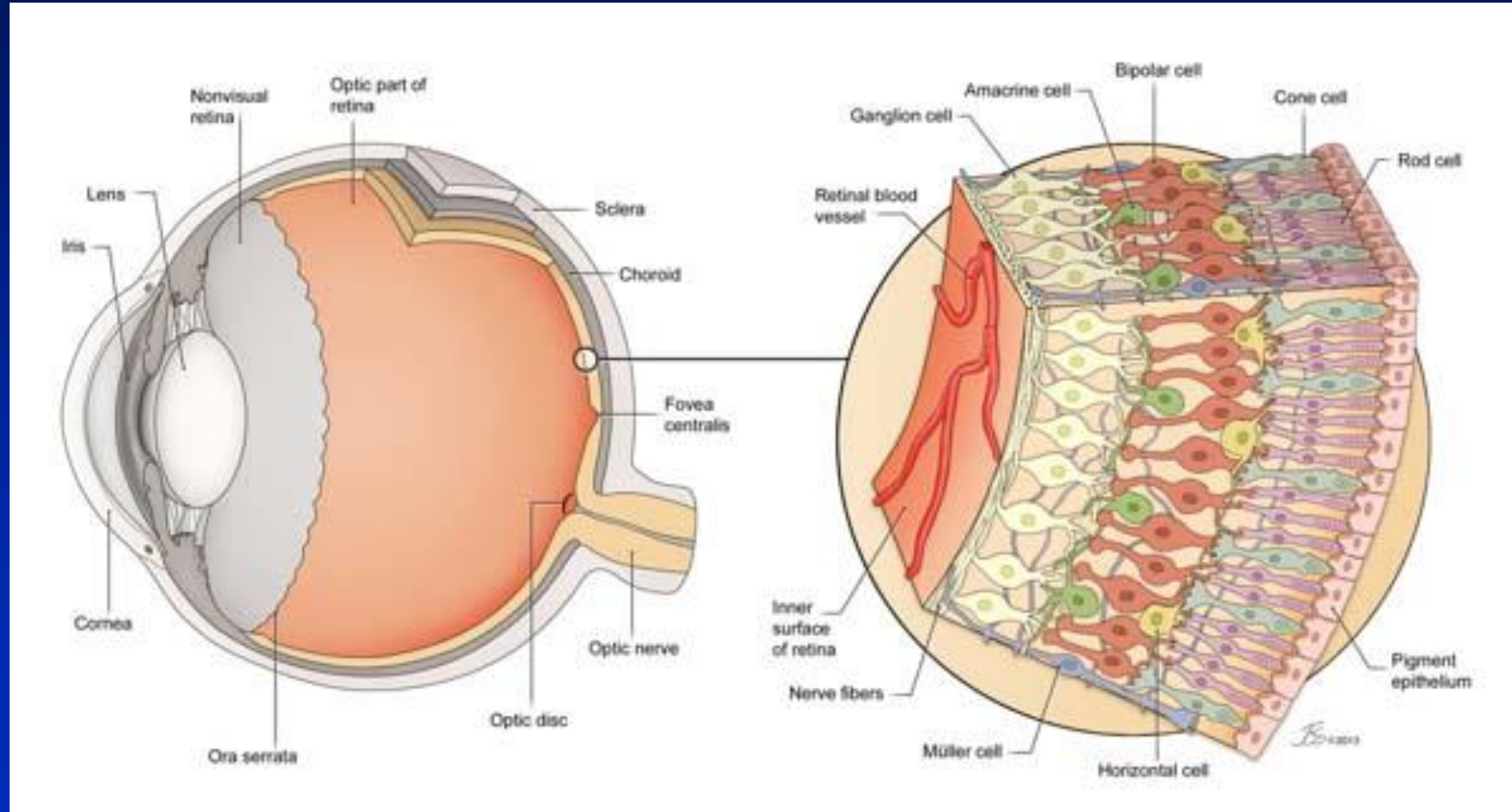
# Visible Light Spectrum



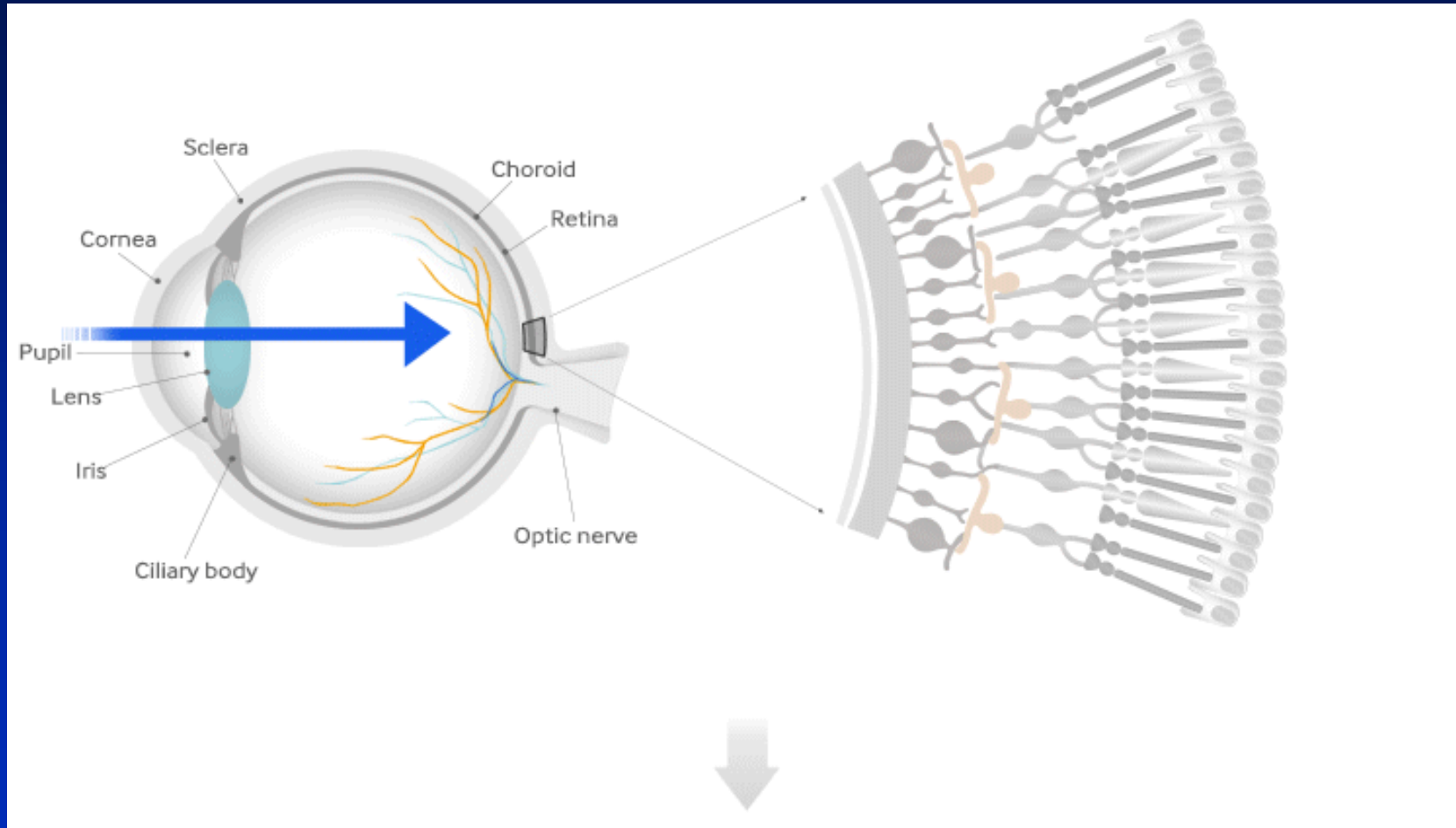
Dominant wavelenghts of the cones of the human receptor system



# Rods and Cones

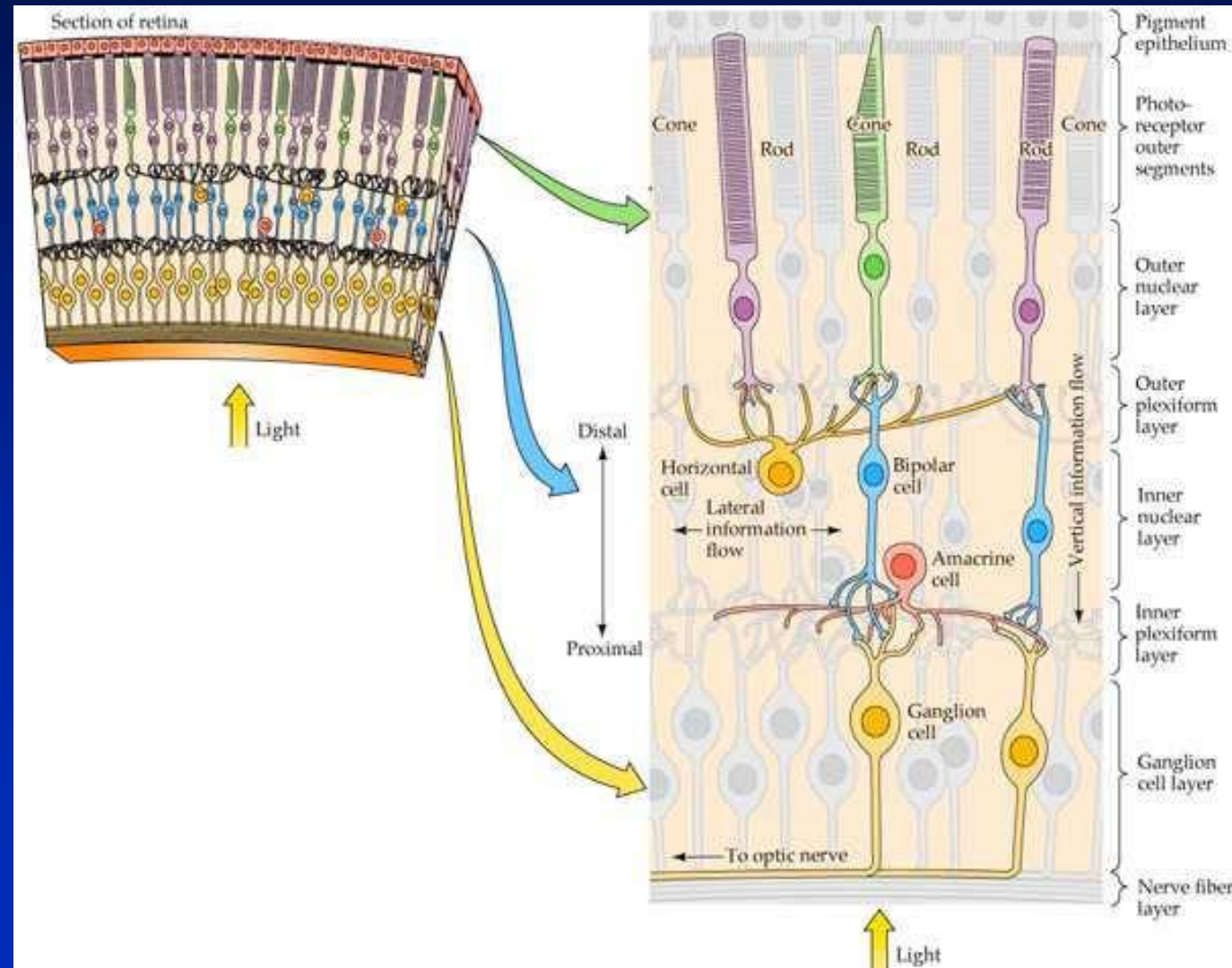


# Color Receptors in the Eye

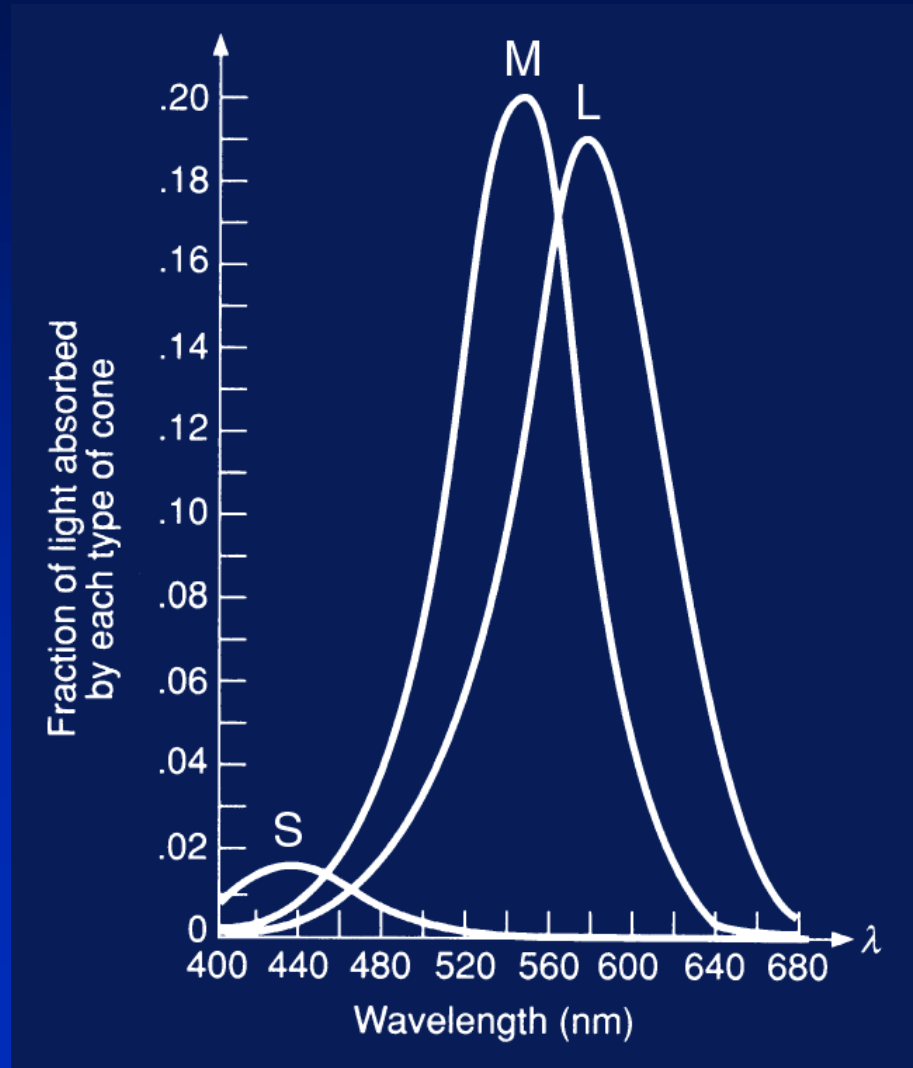




# Rods and Cones



# Cone Responses

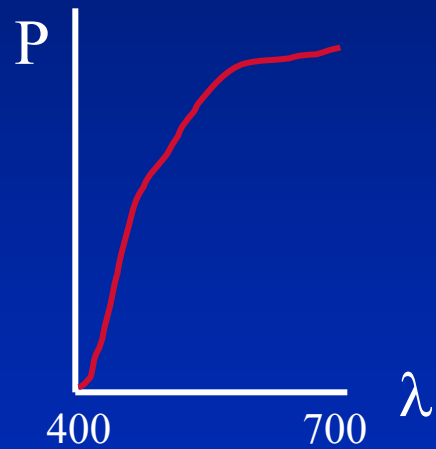


- S,M,L cones have broadband spectral sensitivity
- S,M,L neural response is integrated with respect to  $\lambda$
- results in a trichromatic visual system

# Question?

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- How can we map a *Physical light description* to a *Perceptual color sensation*?

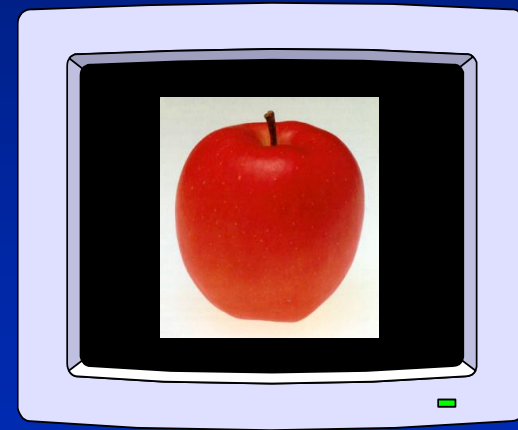


*Physical*

*Perceptual*

# Question?

- How can a TV display reproduce (almost) every color sensation that we can experience using only 3 color phosphors?



R,G,B ?

# Question?

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- How can a printer reproduce (almost) every color sensation that we can experience using only 3 color inks?

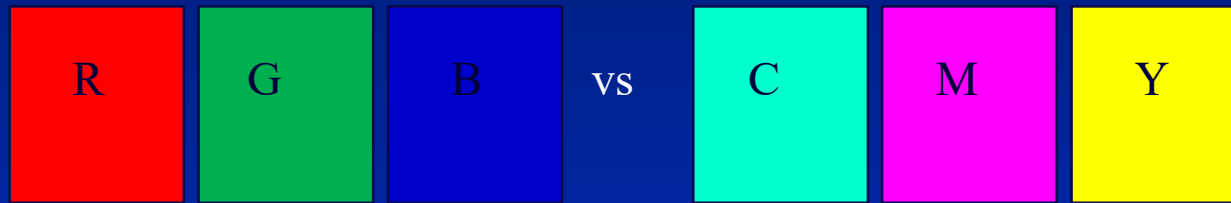


CMY ?

# Question?

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How can we reproduce such a vast range of color using two completely different sets of three primary colors?





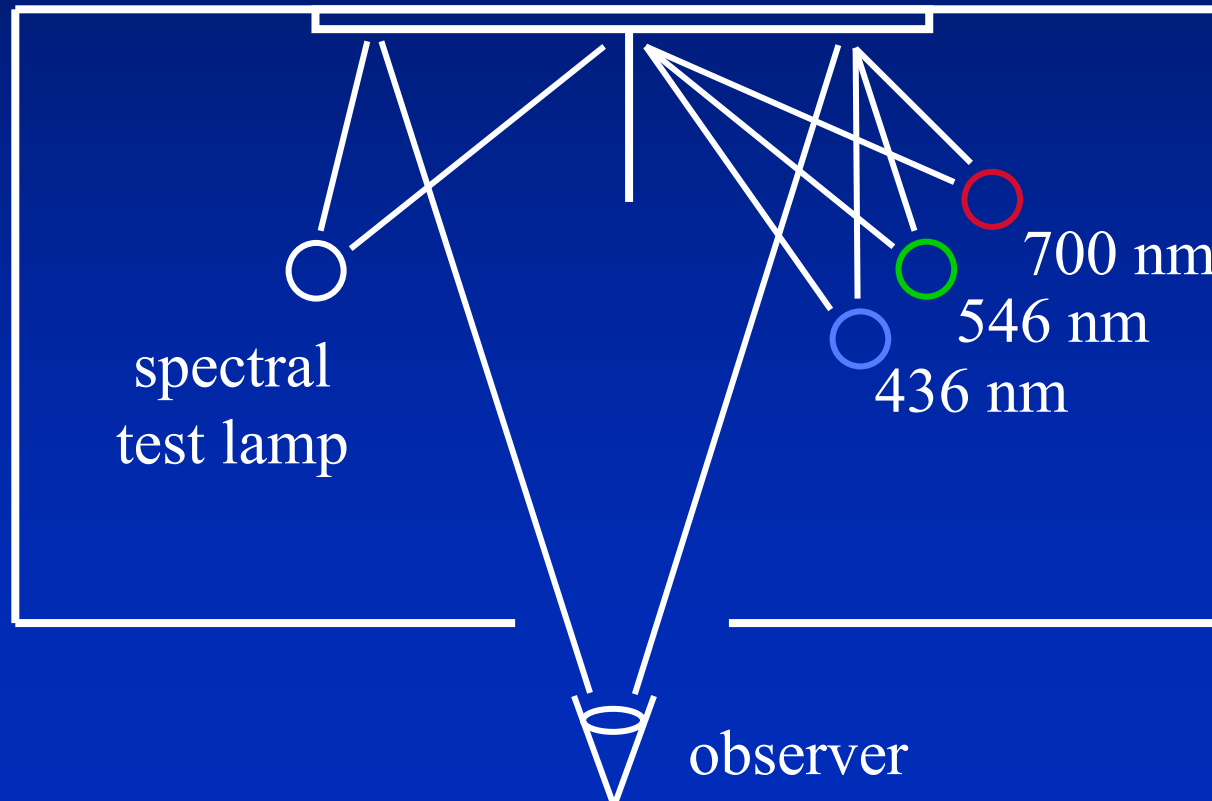
# Grassmann's Color Matching Experiments (1853)

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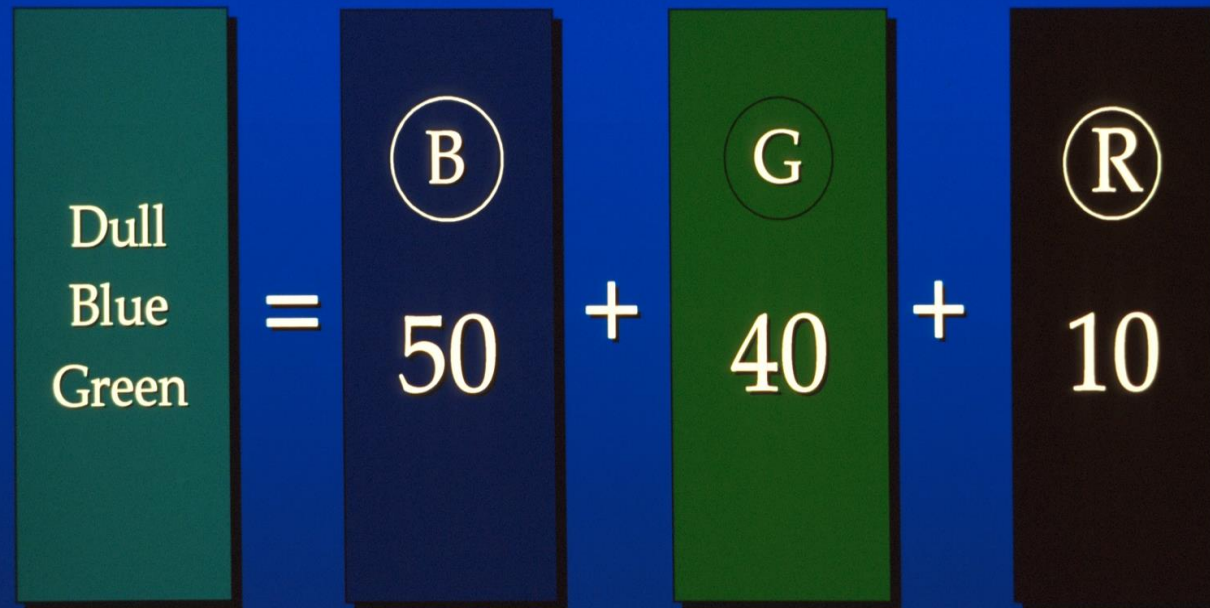
- Roy. S. Berns. Billmeyer and Saltzman's PRINCIPLES OF COLOR TECHNOLOGY, 2000 John Wiley & Sons, Inc.

# Matching a Test Lamp with 3 Primary Lights

- We can match a color sensation from *any* spectrum using only 3 primary colors (R,G,B)

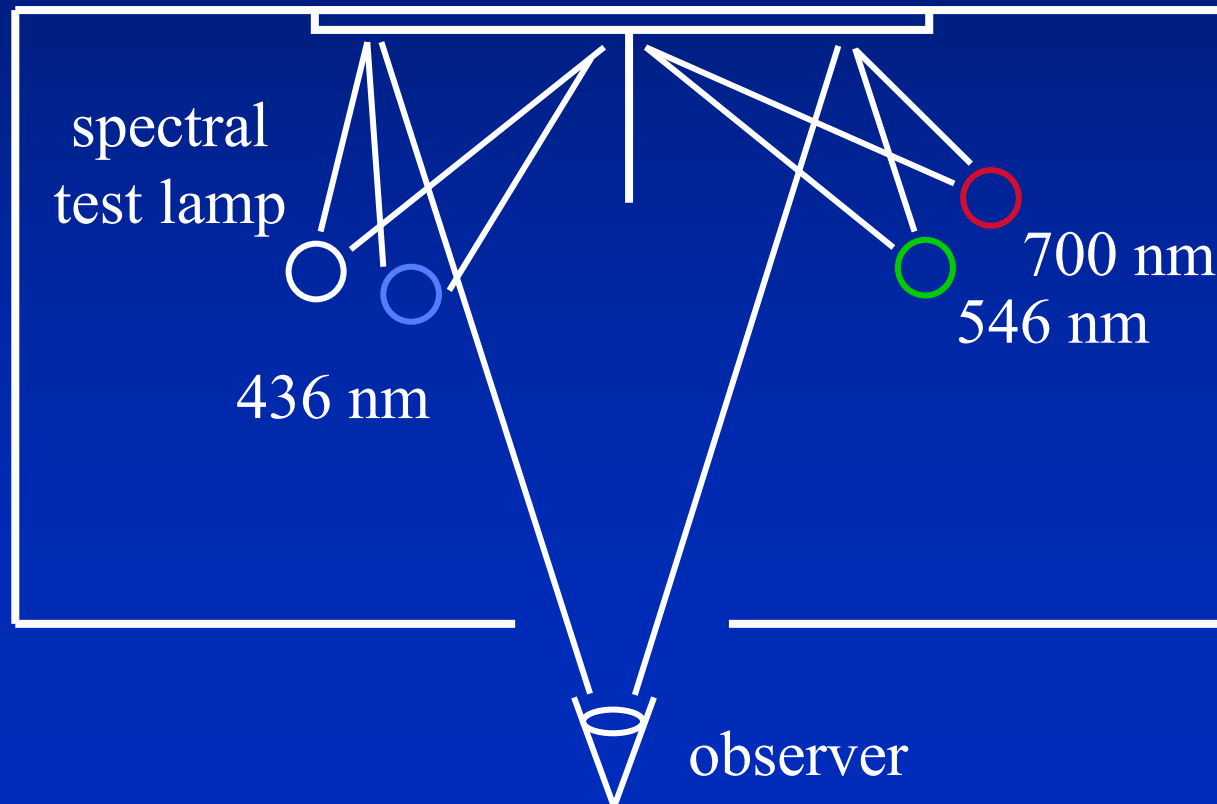


# Matching a Test Lamp with 3 Primary Colors

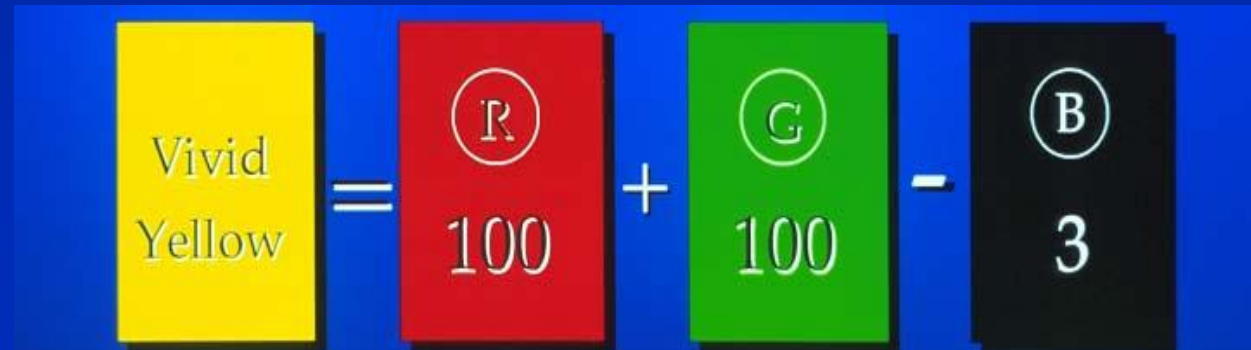
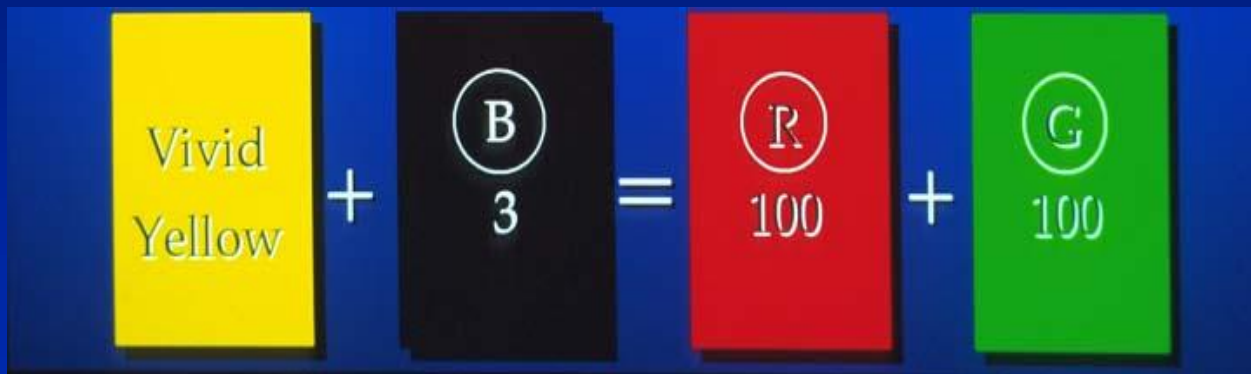
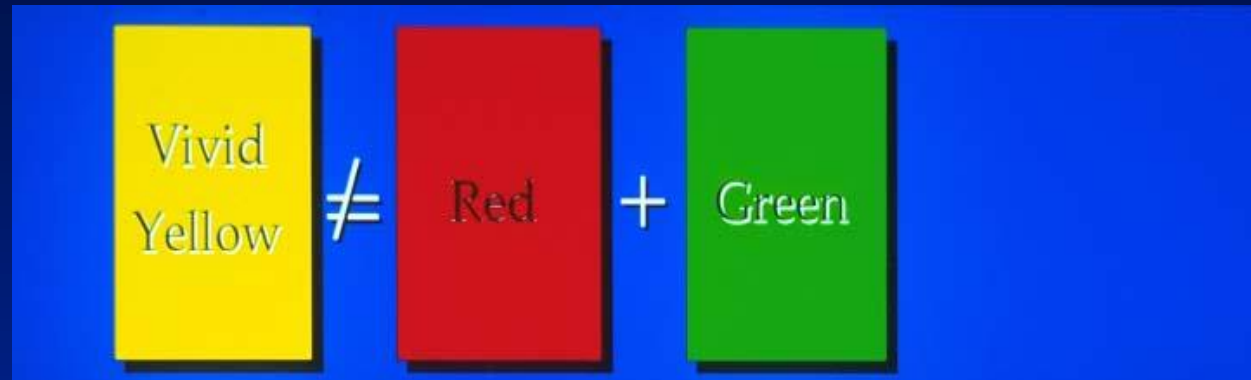


# Matching a Test Lamp with 3 Primary Lights

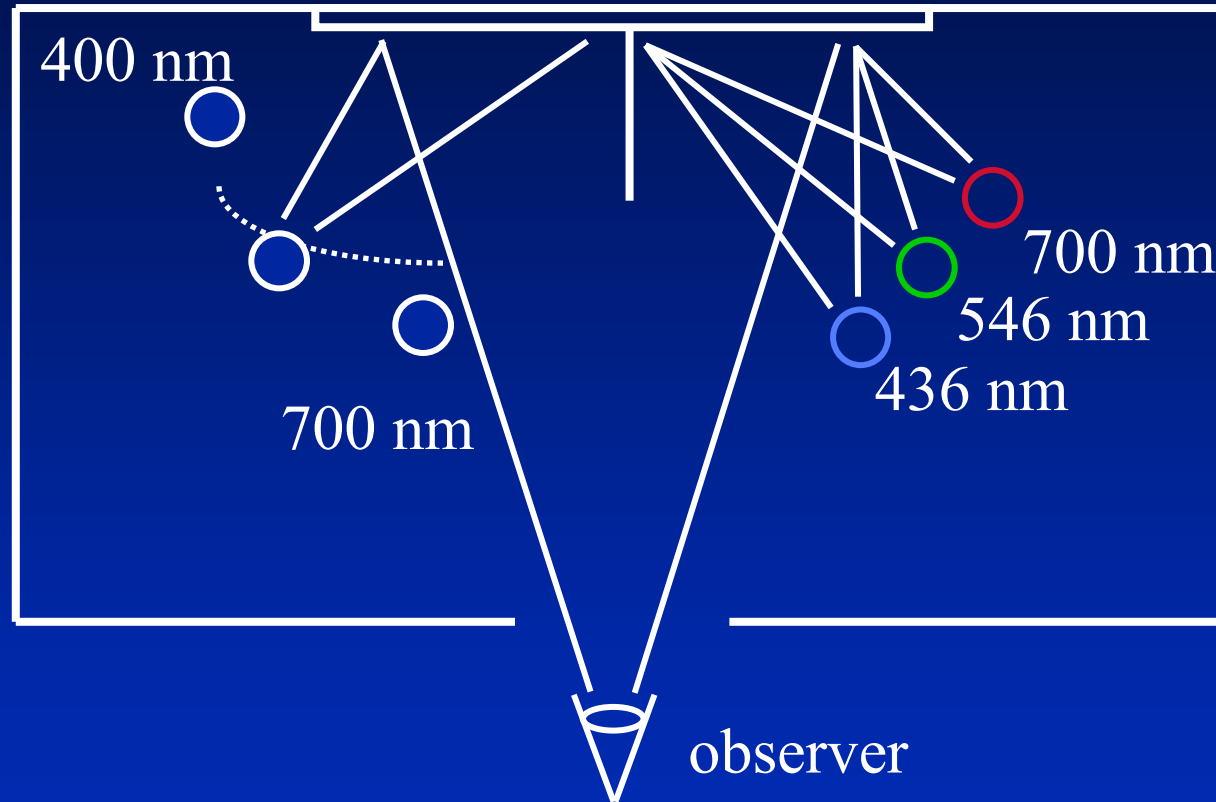
- Need to allow “negative light”
  - Can’t match a bright yellow (Y) light with R,G,B.
  - But can match  $Y + B$  with  $R + G$ .



# Matching a Test Color (Lamp) with 3 Primary Colors

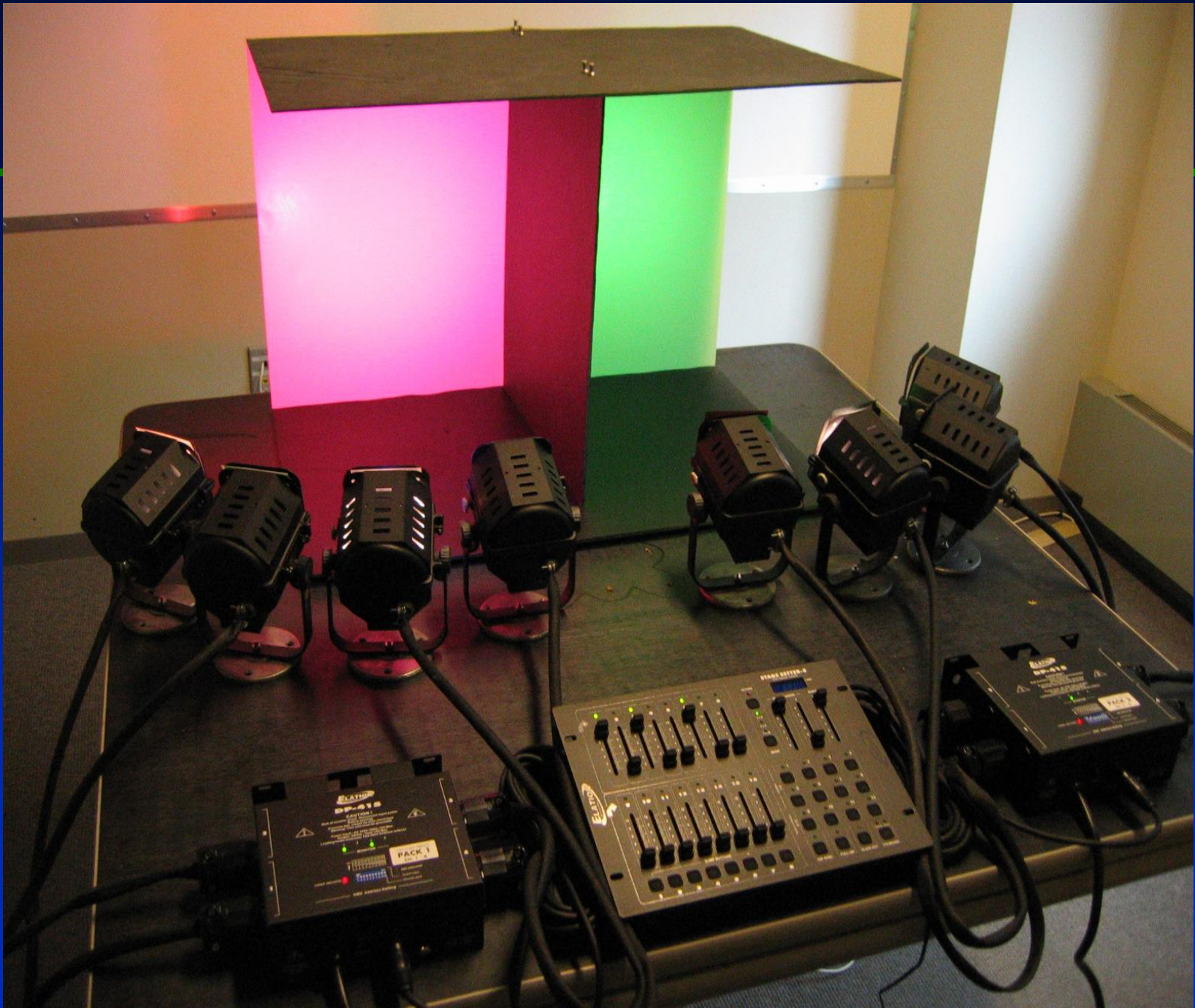


# Experiment to Determine the Response Matching Functions of the Average Human Observer

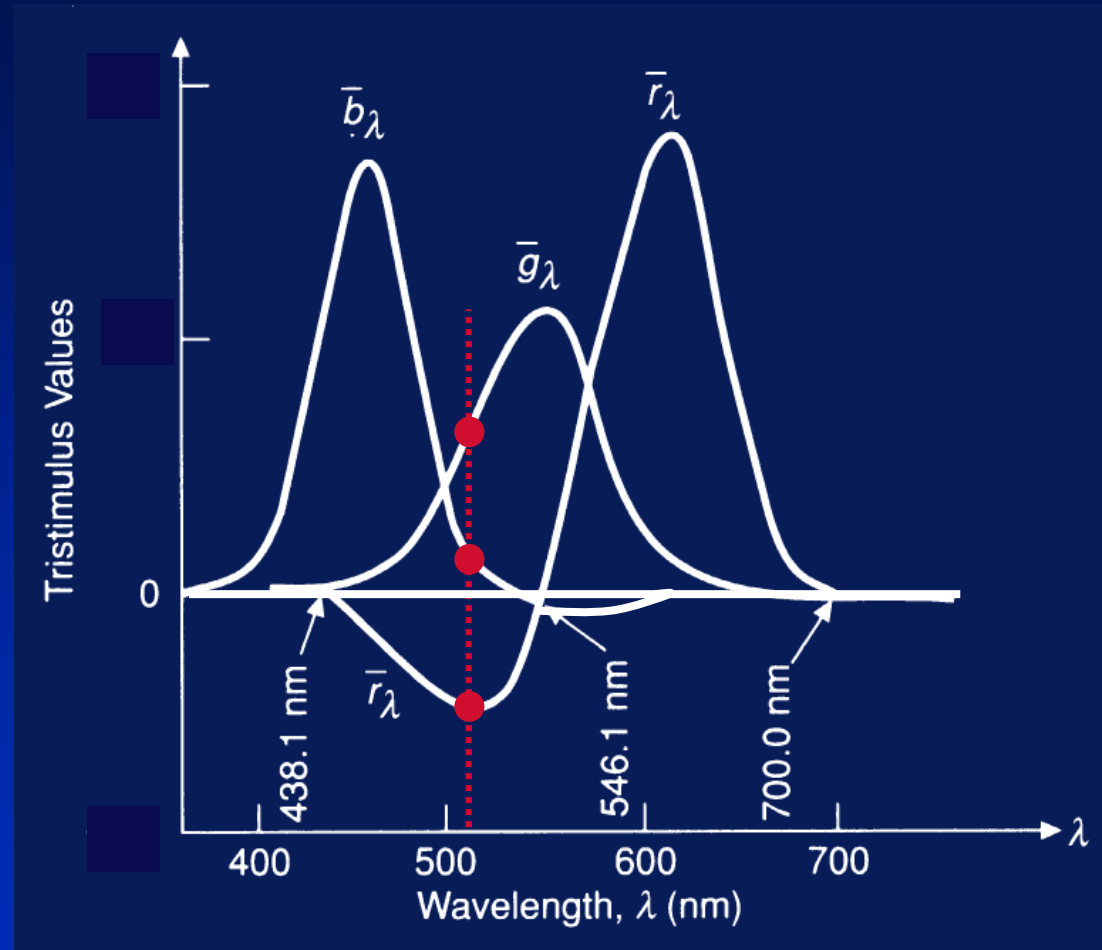


Individually match the RGB primary lights to the unit values of each of the spectral lamps.





# Response Matching Functions of the Average Human Observer



These are the response matching functions of the average human observer for these three primary lights.

# Trichromatic Generalization

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- Many colors can be matched by additive mixtures of suitable amounts of three fixed primary colors.
- Others have to be mixed with a suitable amount of one before it can be matched by the other two.
- All the colors can be matched in one of these two ways:
  - The restriction is that none of the primary colors can be matched by an additive mixture of the other two.

# Trichromatic Generalization

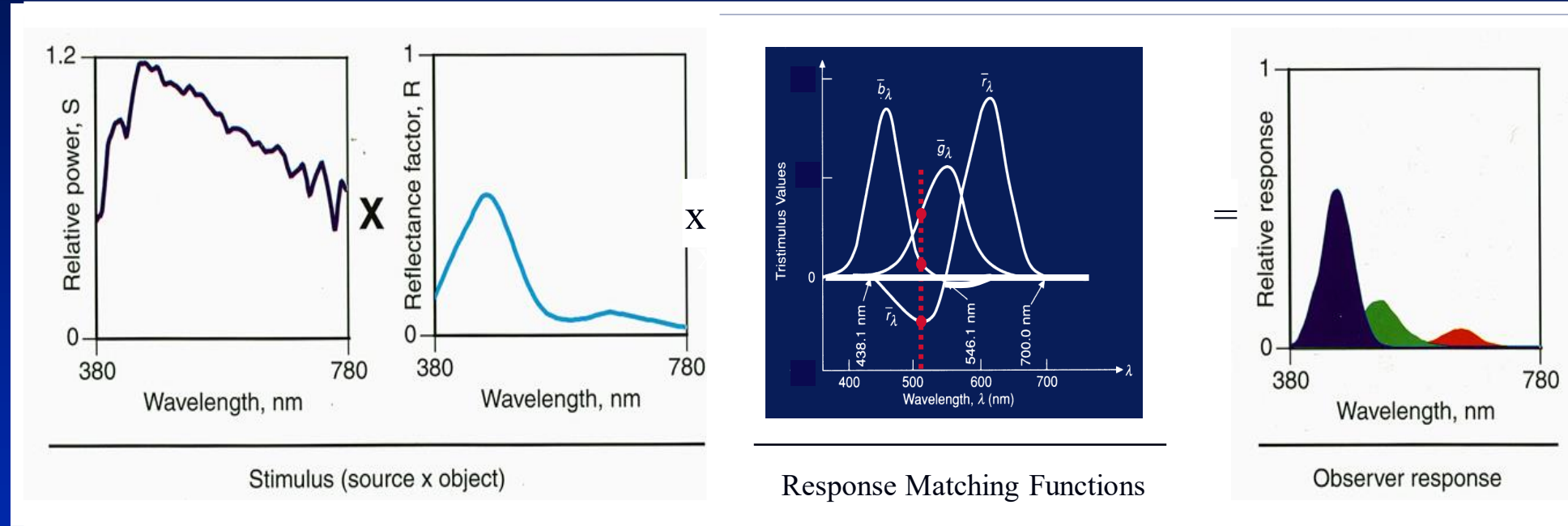
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- **Proportionality** and **additivity** are valid over a large range of observing conditions.

**Proportionality** - If  $A=B$ , then  $kA=kB$

**Additivity**- If  $A=B$ , and  $C=D$ , the  $A+C=B+D$

# Observer Response



# Computing Tristimulus Values with the Response Matching Functions

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- For each test lamp we can compute the equivalent RGB tristimulus values using the color matching functions

$$R = \int P(\lambda) \bar{r}(\lambda) d\lambda$$

$$G = \int P(\lambda) \bar{g}(\lambda) d\lambda$$

$$B = \int P(\lambda) \bar{b}(\lambda) d\lambda$$



# Comments on Response Matching Functions

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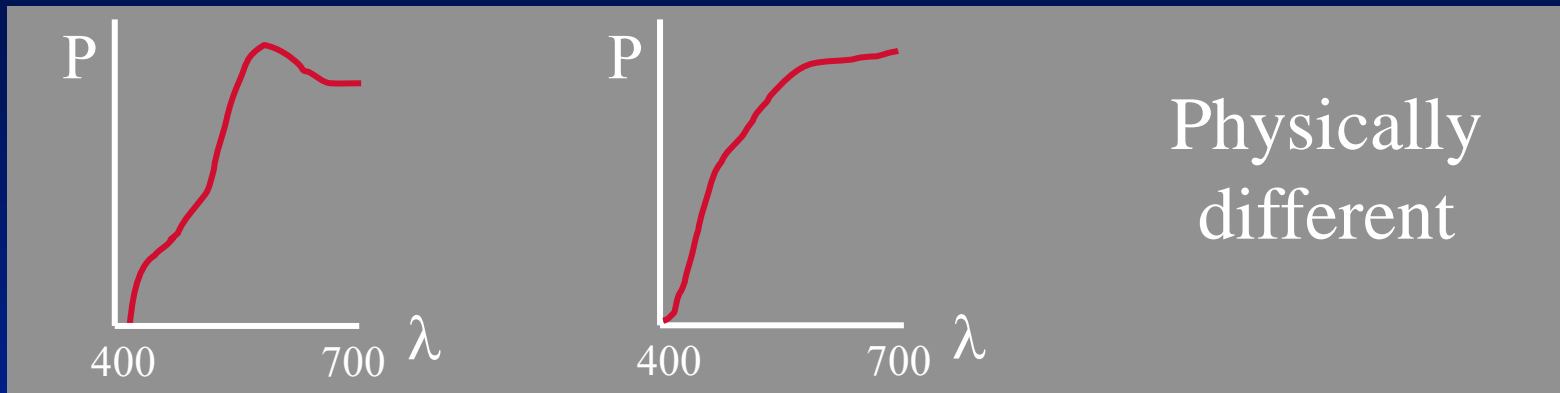
- Note that knowing the spectral distributions of the primary light sources and the response matching functions of the average human observer, we can then represent a large range of colors with any three primary light sources. (Monitors, cell phones, and printers).
- Perhaps most important, is the fact that these are perceptual spaces because a human observer is within the experimental testing loop.
- All of these tests have been conducted in a dark room and thus do not consider the effect of the illumination within the external environment.

# Metamer

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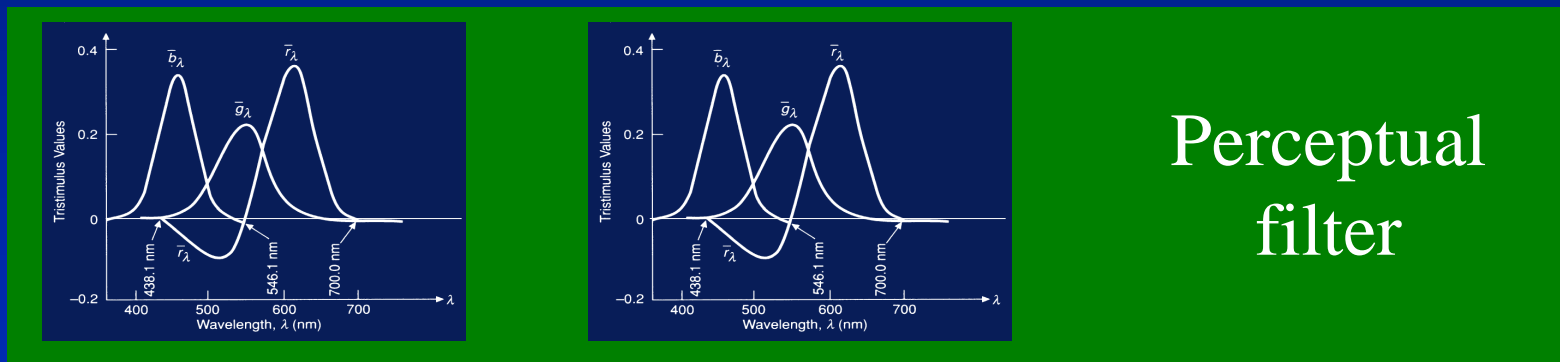
A metamer is a phenomenon in which two spectrally different stimuli match to a given observer.

# Metamers



×

×



$R, G, B$

=

$R, G, B$

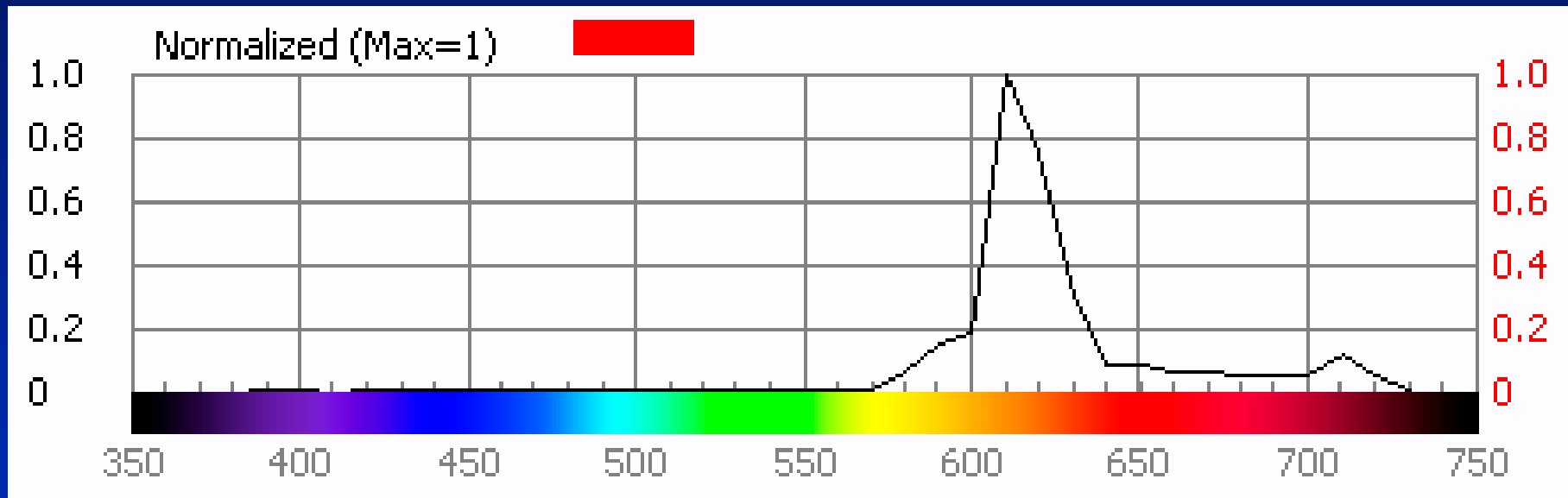
Perceptually equal

# Metamers

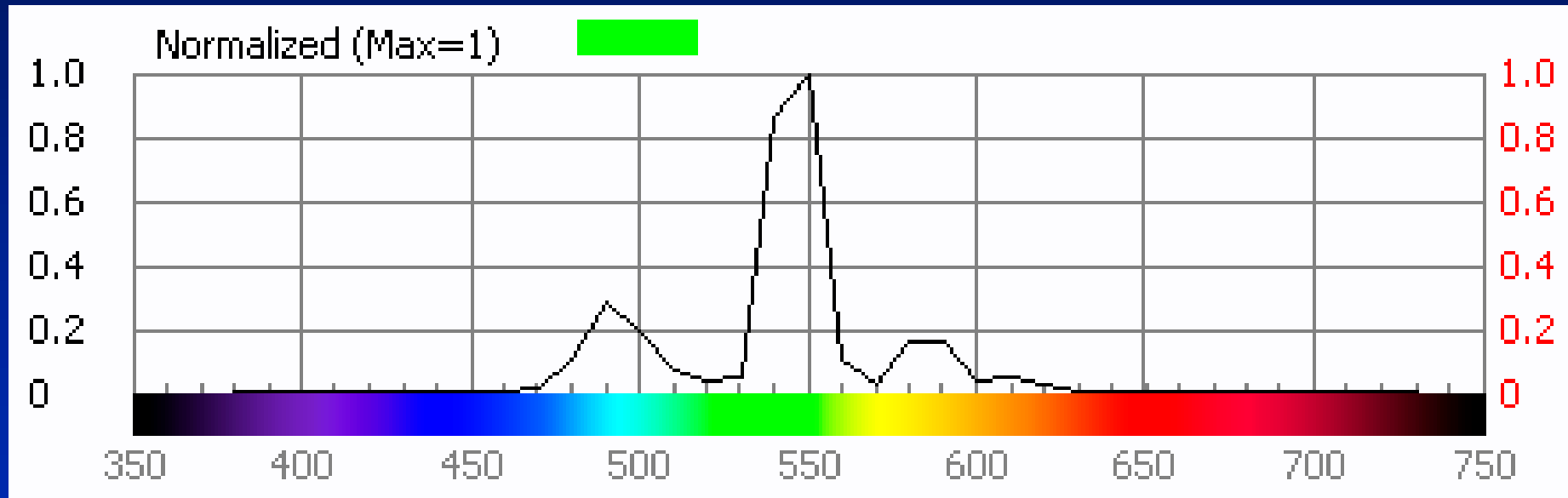
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- Trichromacy, perhaps the most important property of the visual system, leads to metamerism. (Grassman 1853)
- Metamerism is a phenomenon in which spectrally different stimuli match to a given observer.
- Because of metamerism, color reproduction is possible.
- Stimuli do not have to have identical spectral properties in order to have a perceptual color match.

# Typical LCD spectral radiance distribution

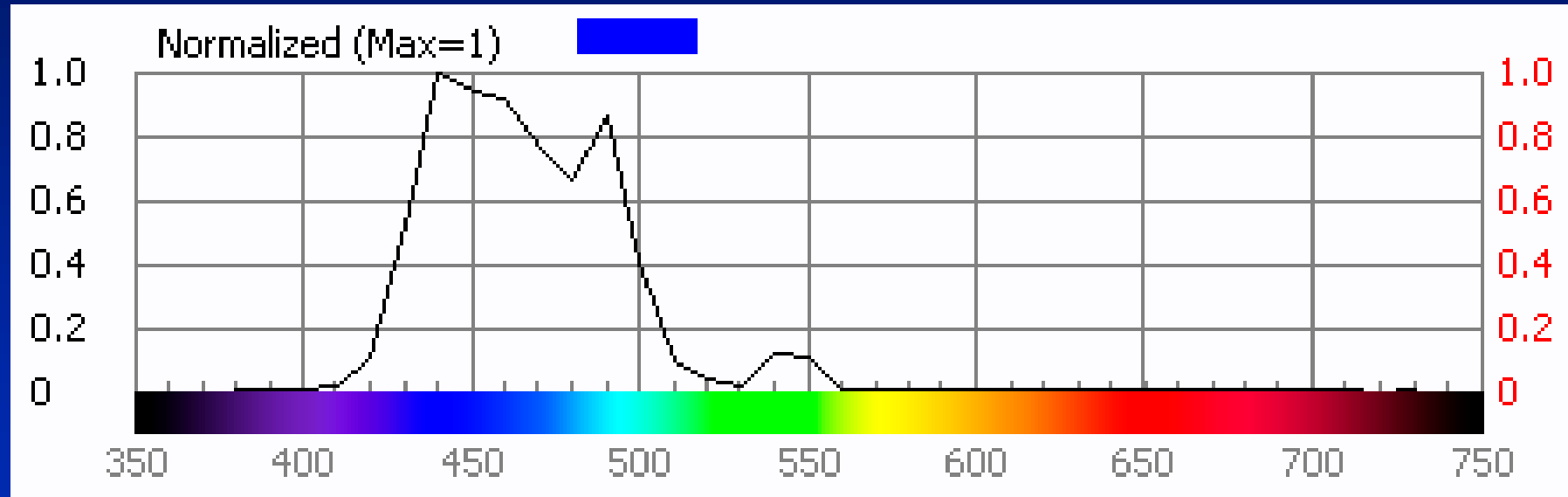


# Typical LCD spectral radiance distribution





# Typical LCD spectral radiance distribution



# Typical LCD spectral radiance distribution

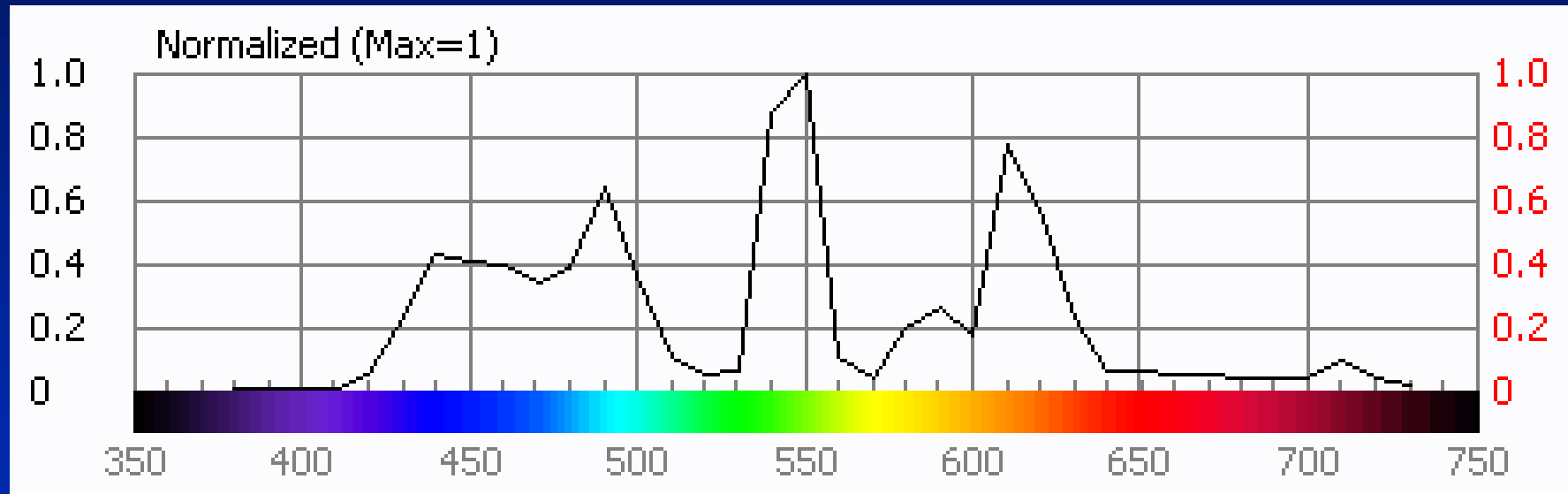
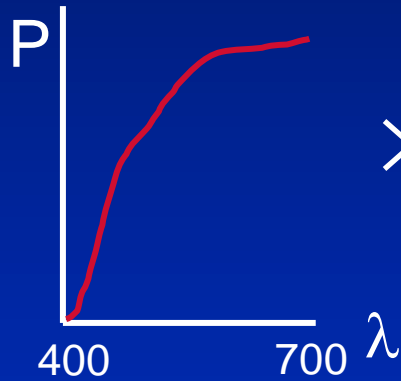
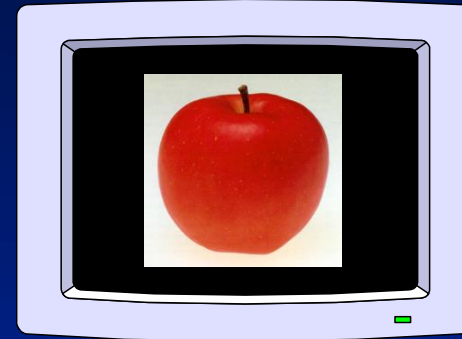
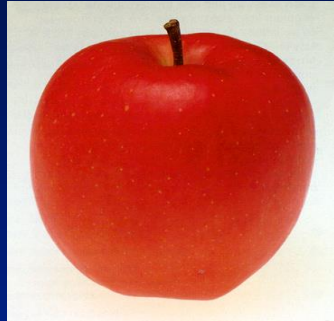
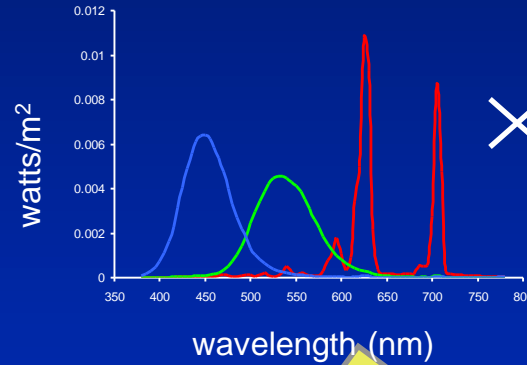
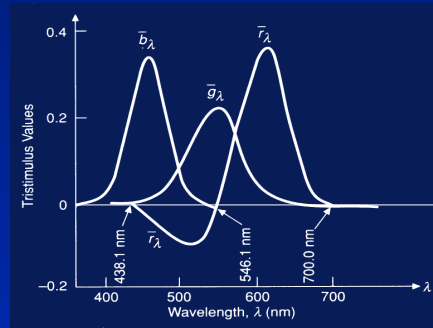


Figure #3 -- <http://www.marcelpatek.com/LCD.html>

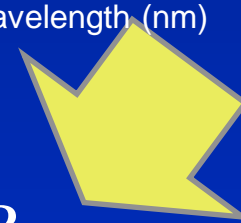
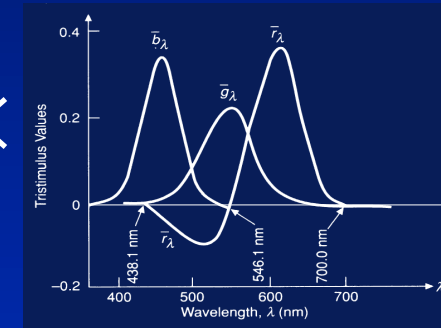
# Taking Advantage of Metamers



×




×



$$R, G, B = R, G, B$$

**Visual match**

# Color Vision 2



## *Color Vision 2. Color Matching*

Craig Blackwell, MD  
*Fellow American Academy of Ophthalmology  
Diplomate American Board of Ophthalmology*

*Lighthouse Beach, CBlackwell, Jan 2008*

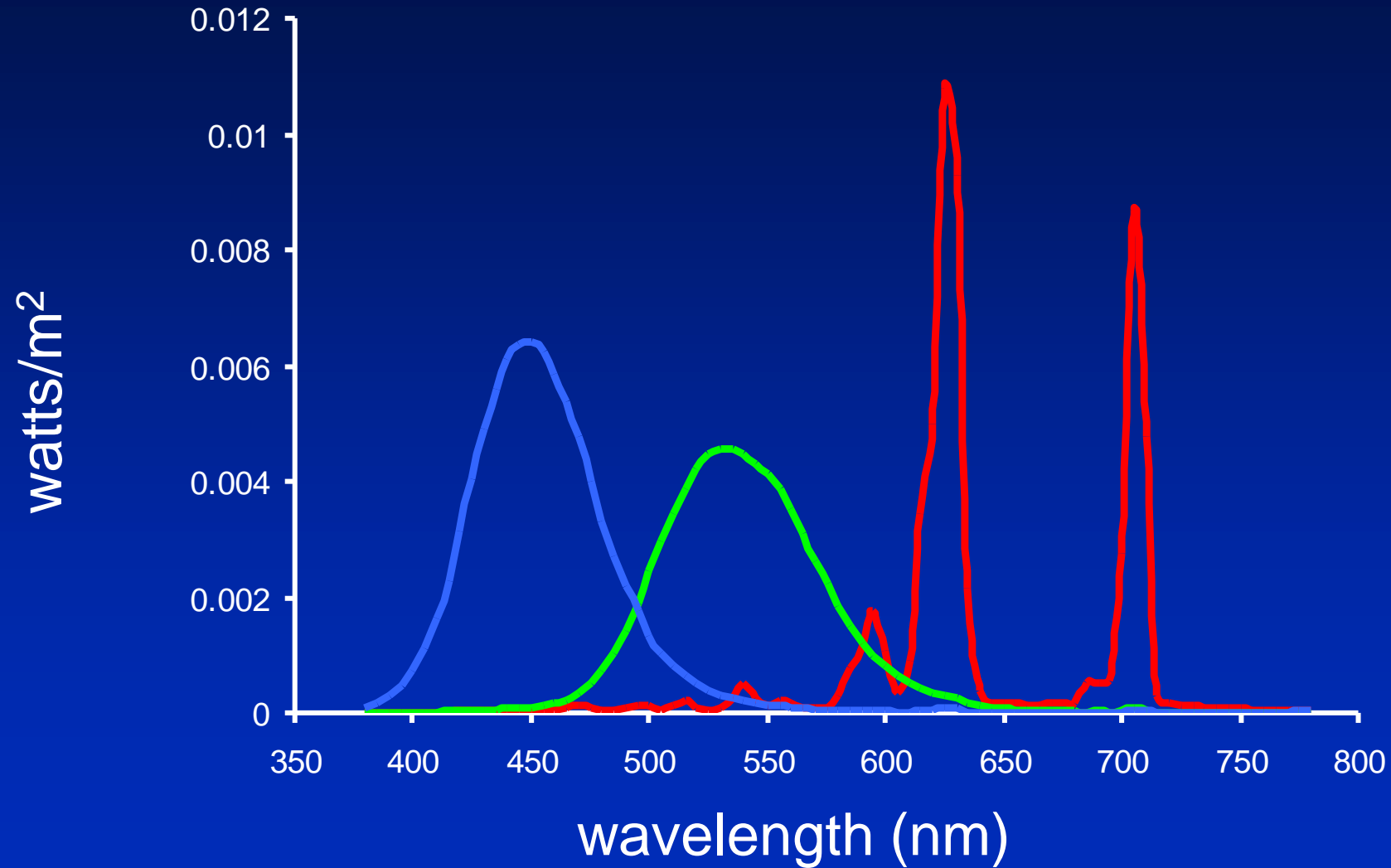
End. . .

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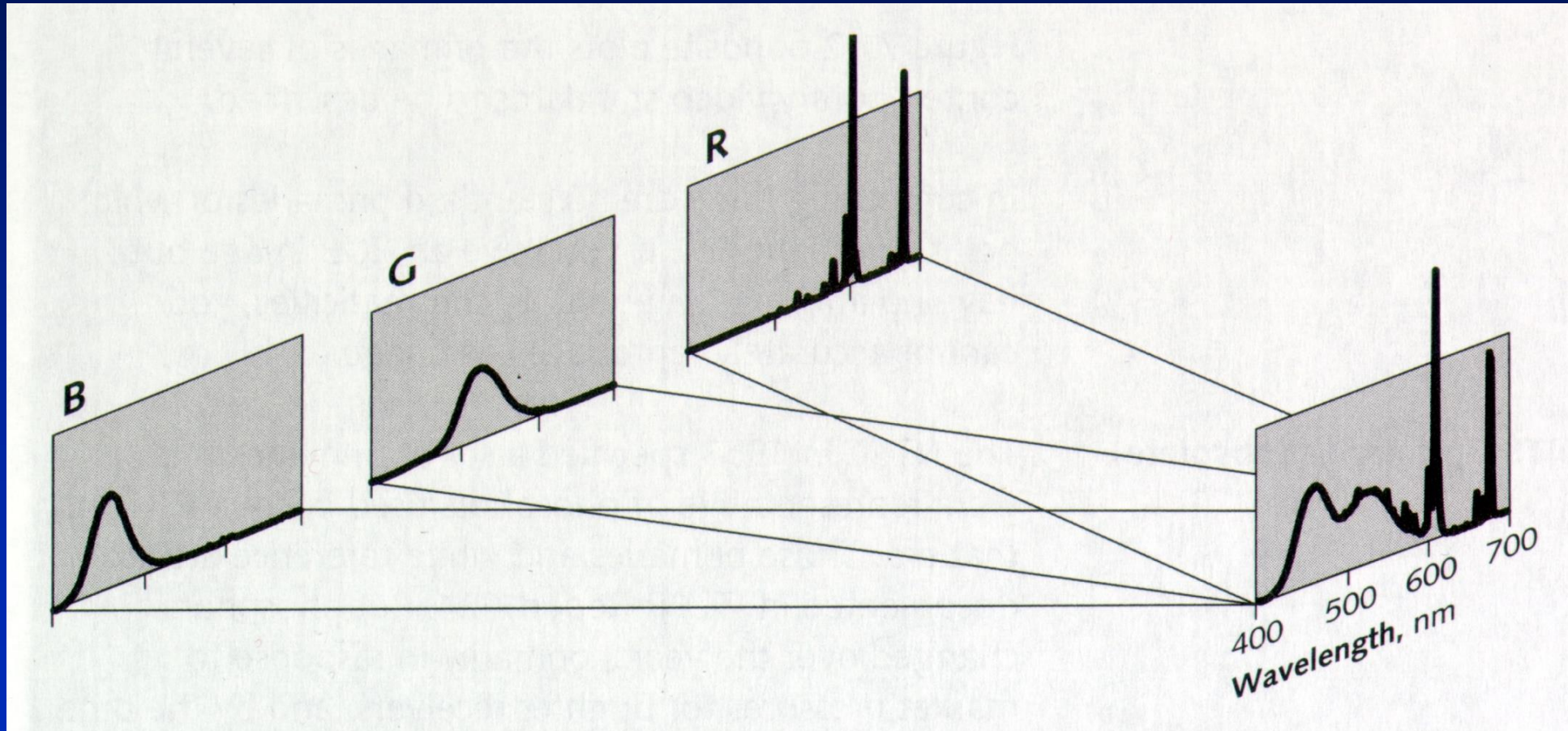




# Vacuum Tube Monitor Phosphors

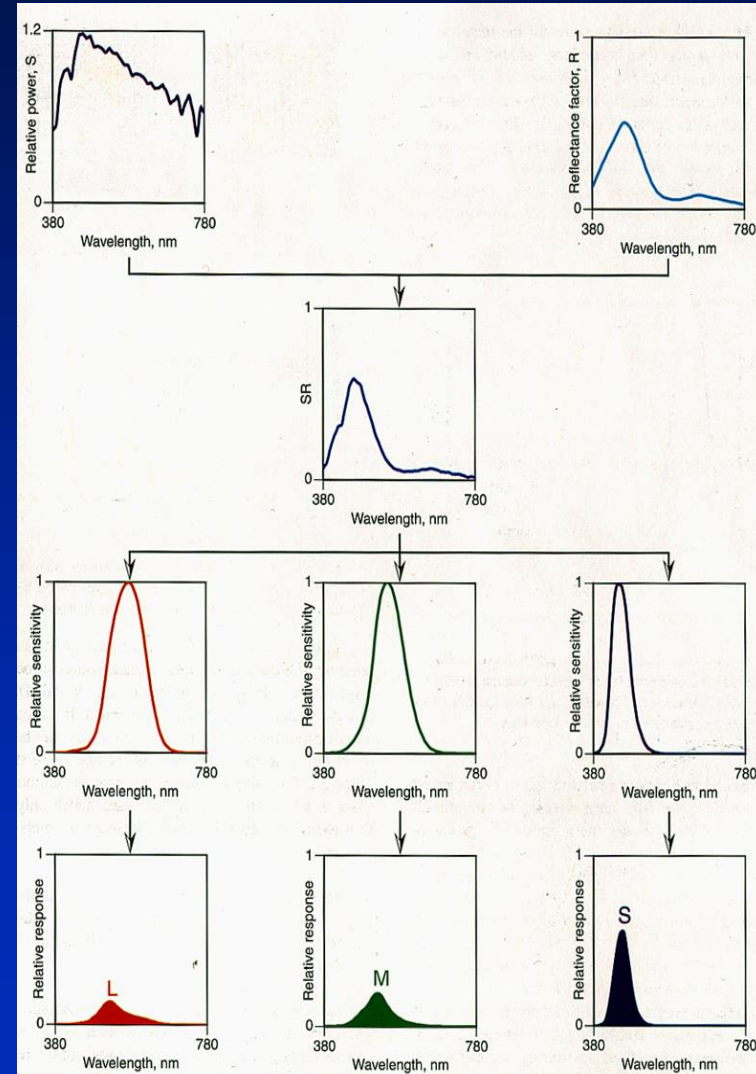


# Combining Monitor Phosphors with Spatial Integration

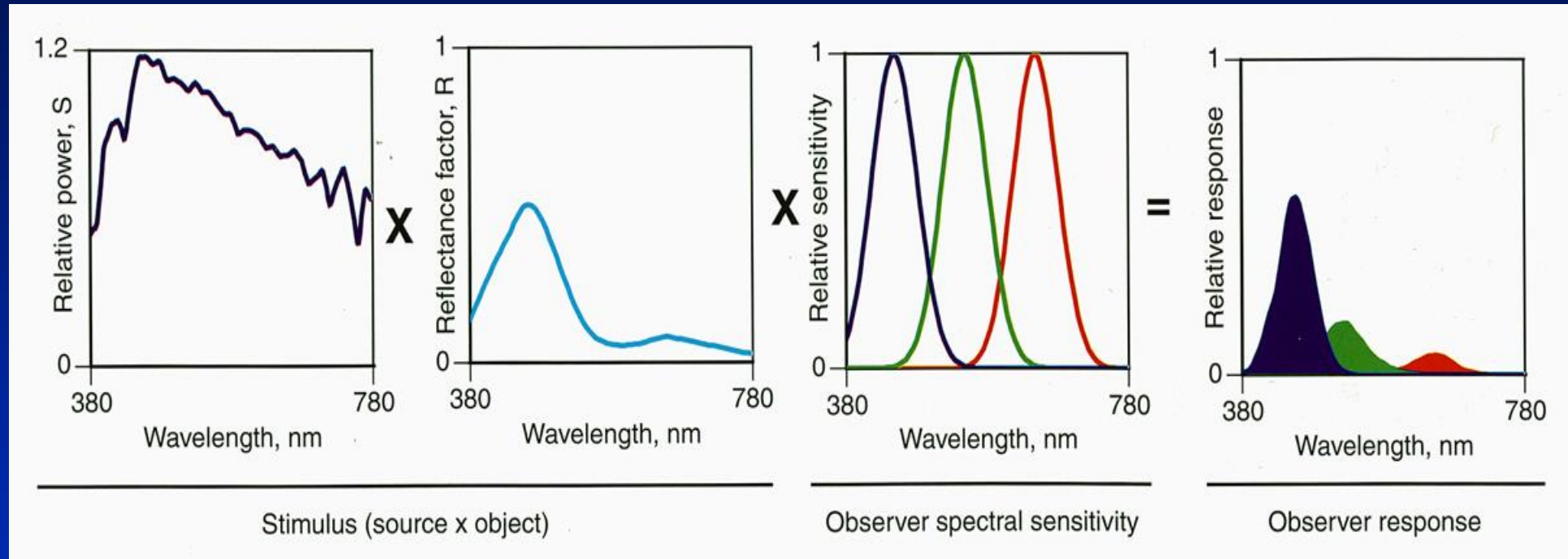


# Observer Response

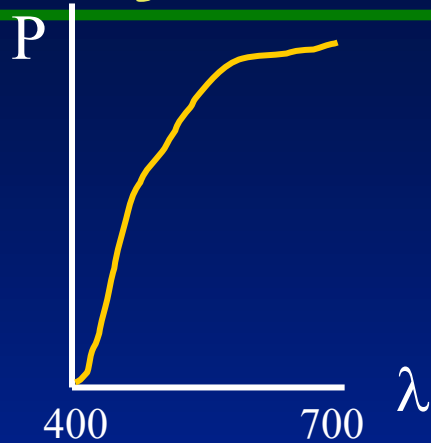
The integrated L, M, and S responses that result from the light entering the eye from an illuminated object. This can be calculated as the product of the spectral properties of the light source, the object, and the observer's sensitivities, followed by integration over wavelength, essentially, calculating the areas under the last row of curves.



# Observer Response



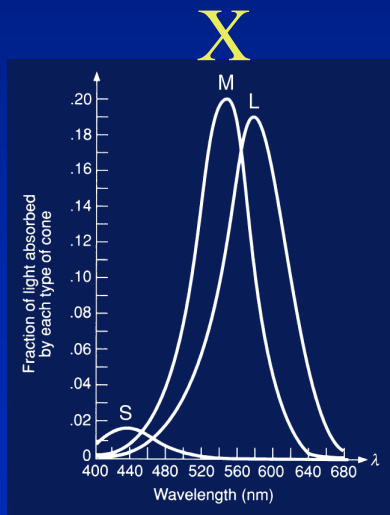
# Trichromacy



$$S = \int P(\lambda) s(\lambda) d\lambda$$

$$M = \int P(\lambda) m(\lambda) d\lambda$$

$$L = \int P(\lambda) l(\lambda) d\lambda$$



$S, M, L$

# Printer Inks

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Yellow

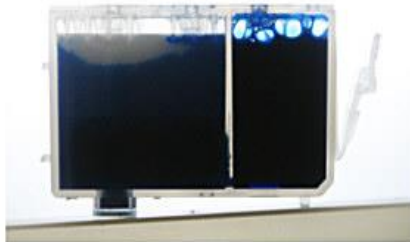


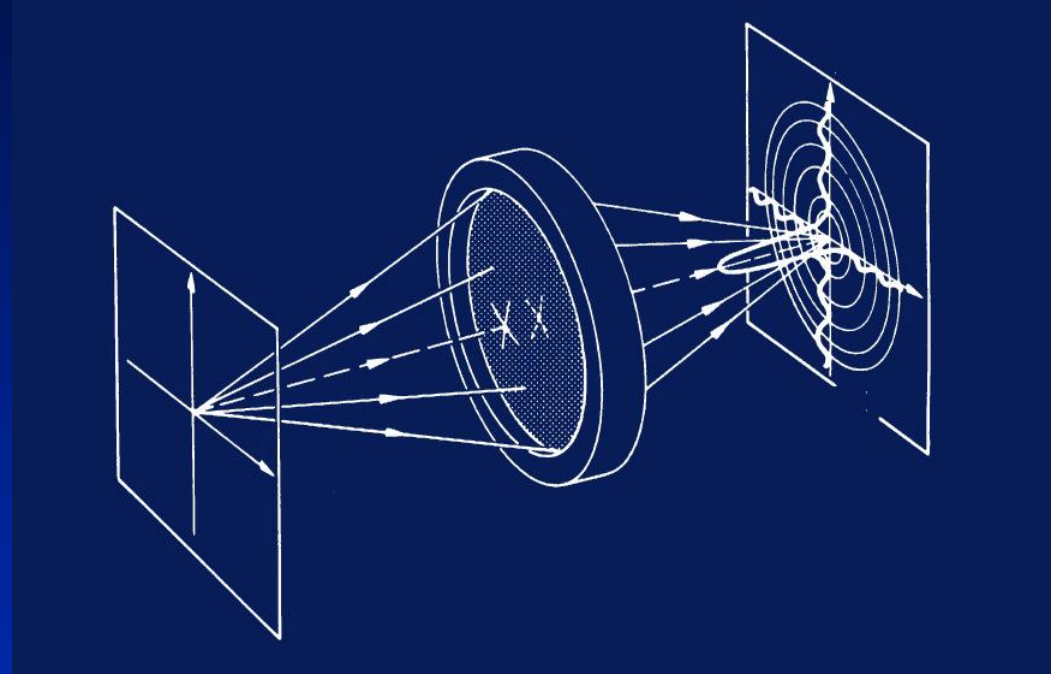
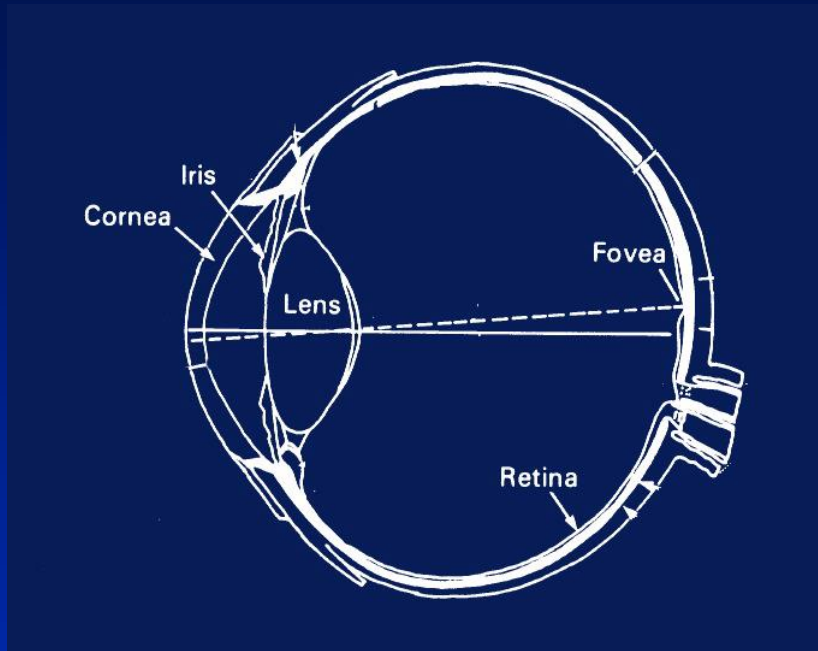
Photo Cyan



Photo Magenta



## Formation of the Retinal Image



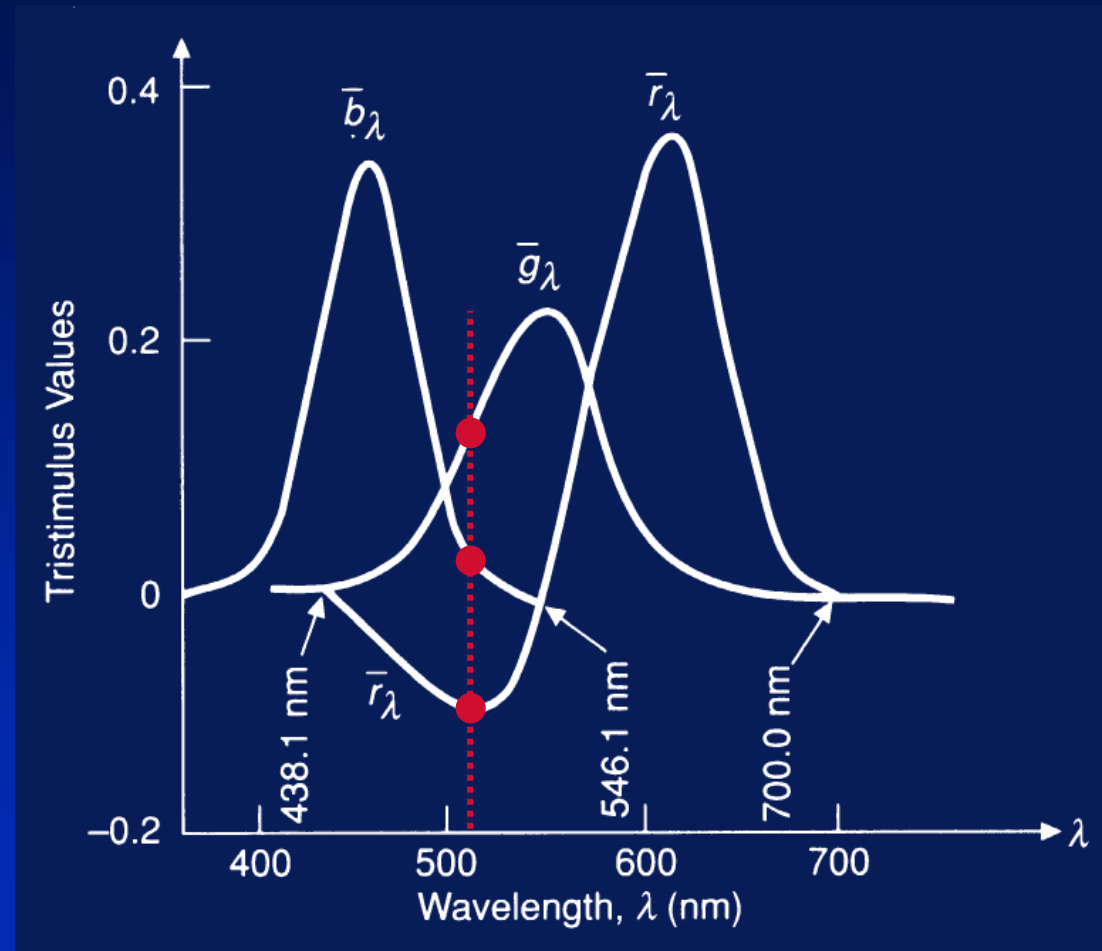
- point spread function (PSF): luminance distribution produced by imaging a point source

Left figure adapted from: Atkinson, Steven's Handbook of Experimental Psychology © Wiley 1988.

Right figure adapted from: Hecht, Optics © Addison-Wesley 1974.



# Response Matching Functions



These are the response matching functions of the average human observer for these three primary lights.

## Emitted Light

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$$P = \sum_{\lambda} E_{\lambda}$$

$P$  = energy reaching the eye at all wavelengths

$E_{\lambda}$  = emitted light energy at each wavelength

## Reflected Light

---

$$P = \sum_{\lambda} E_{\lambda} \quad (\text{Emitted Light})$$

$$P = \sum_{\lambda} E_{\lambda} \cdot \rho_{\lambda}$$

$P$  = energy reaching the eye at all wavelengths

$E_{\lambda}$  = emitted light energy at each wavelength

$\rho_{\lambda}$  = reflected light energy at each wavelength

# Transmitted Light

---

$$P = \sum_{\lambda} E_{\lambda} \quad (\text{Emitted Light})$$

$$P = \sum_{\lambda} E_{\lambda} \cdot \rho_{\lambda} \quad (\text{Reflected Light})$$

$$P = \sum_{\lambda} E_{\lambda} \cdot T_{\lambda} \quad (\text{Transmitted Light})$$

$T_{\lambda}$  = transmitted light energy at each wavelength

# Computing Tristimulus Values with the Response Matching Functions

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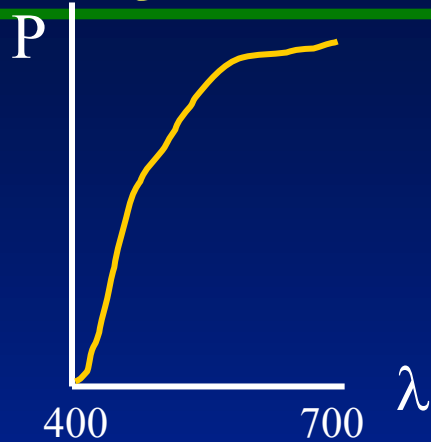
- For each test lamp we can compute the equivalent RGB tristimulus values using the color matching functions

$$R = \int P(\lambda) \bar{r}(\lambda) d\lambda$$

$$G = \int P(\lambda) \bar{g}(\lambda) d\lambda$$

$$B = \int P(\lambda) \bar{b}(\lambda) d\lambda$$

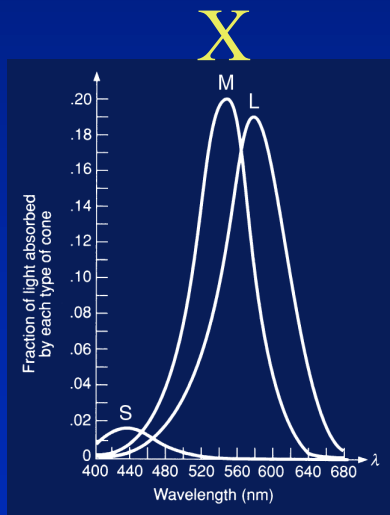
# Trichromacy



$$S = \int P(\lambda)s(\lambda)d\lambda$$

$$M = \int P(\lambda)m(\lambda)d\lambda$$

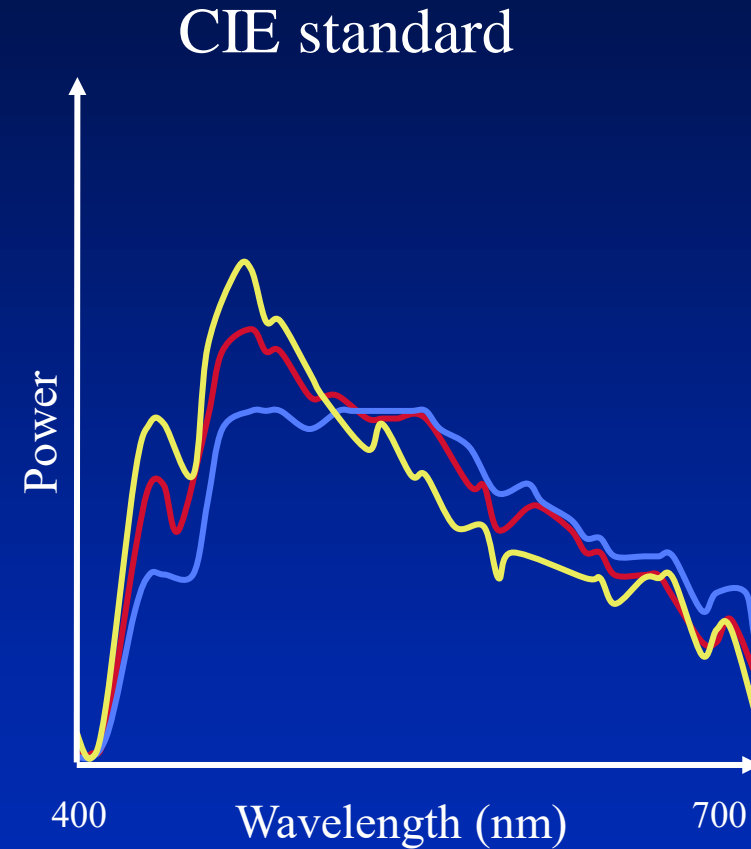
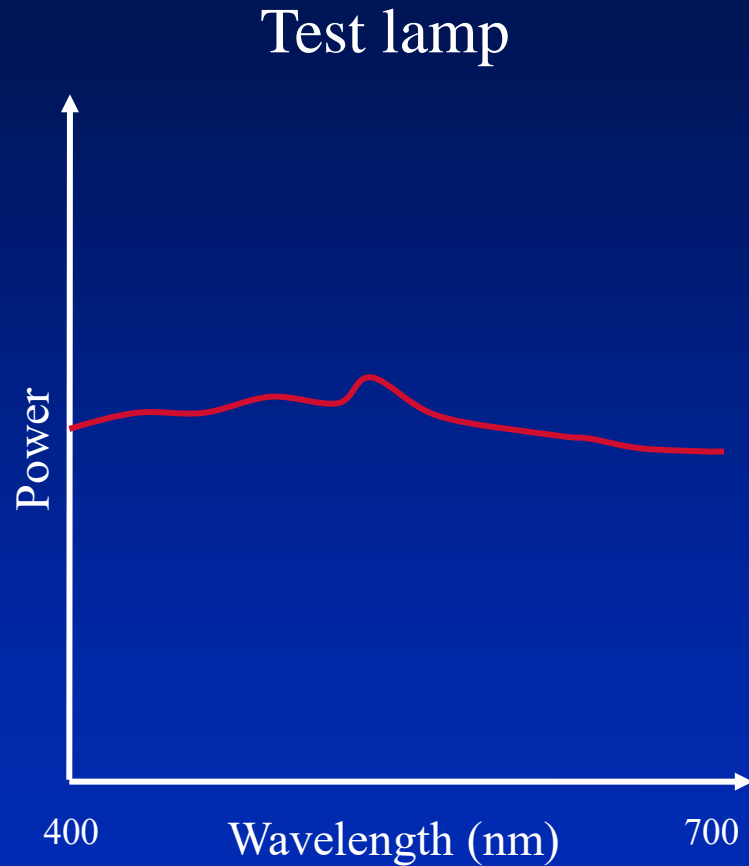
$$L = \int P(\lambda)l(\lambda)d\lambda$$



$S, M, L$

- produces metamers

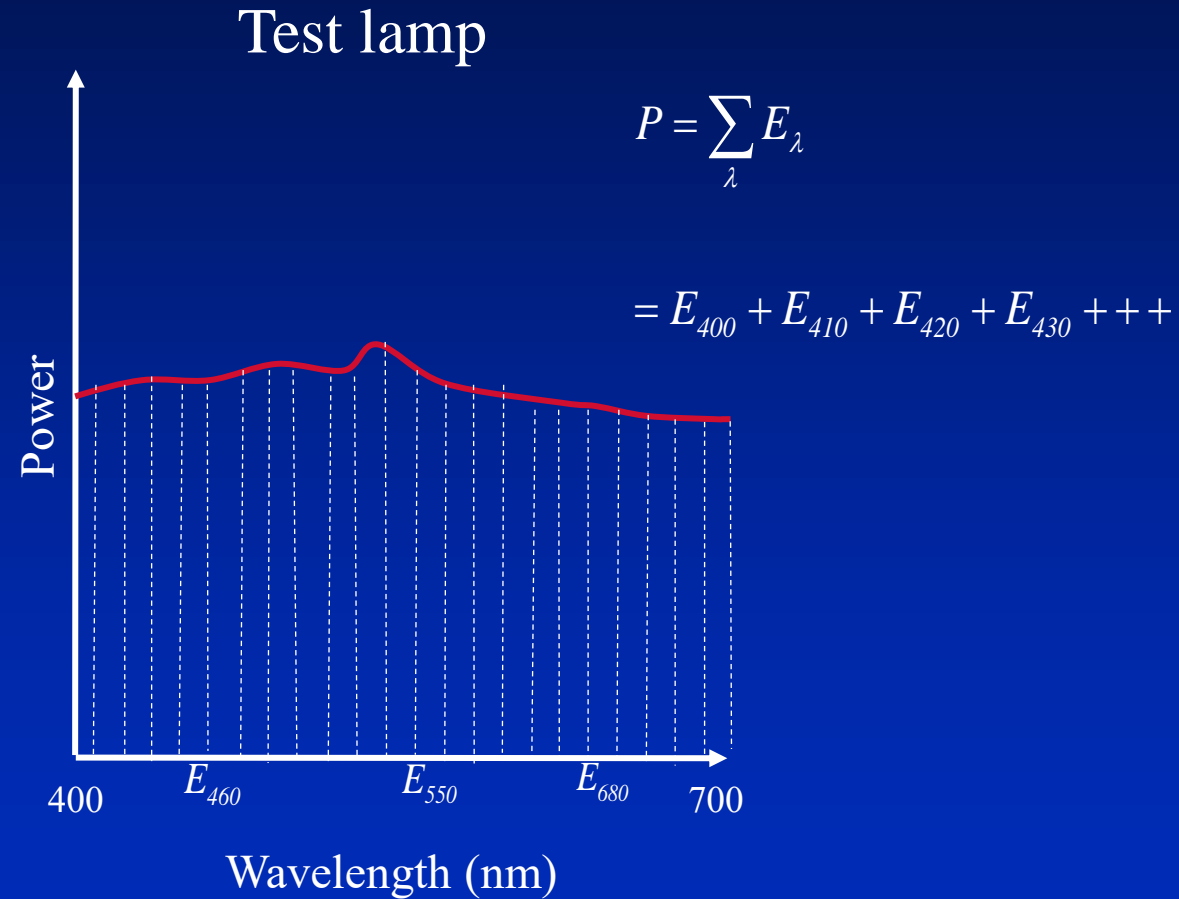
# Spectral Distributions (Wavelengths) of Emissive Light Sources



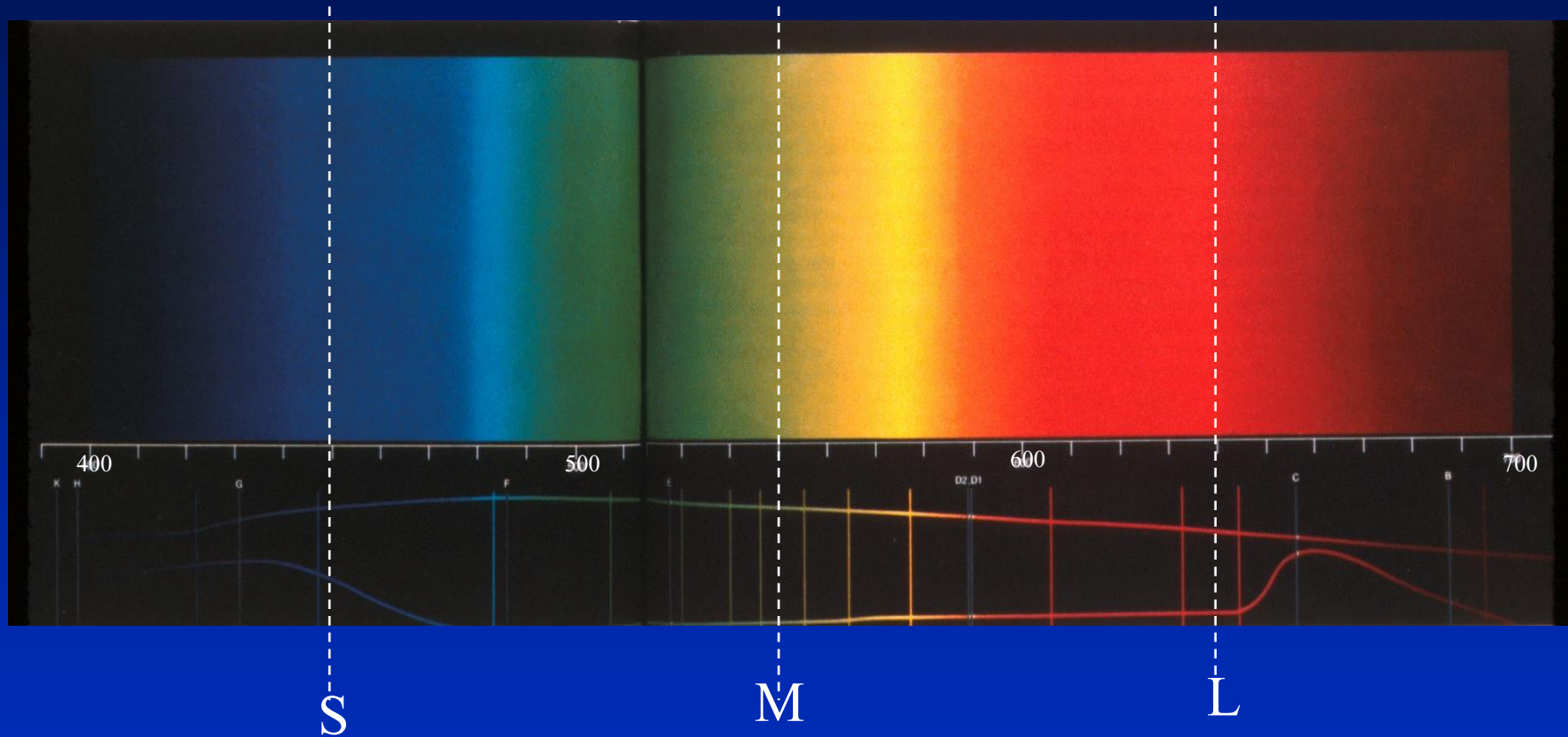
- D<sub>55</sub>: typical sunlight
- D<sub>65</sub>: typical average daylight
- D<sub>75</sub>: typical 'north-sky' light



# Spectral Distributions of Emissive Light Sources

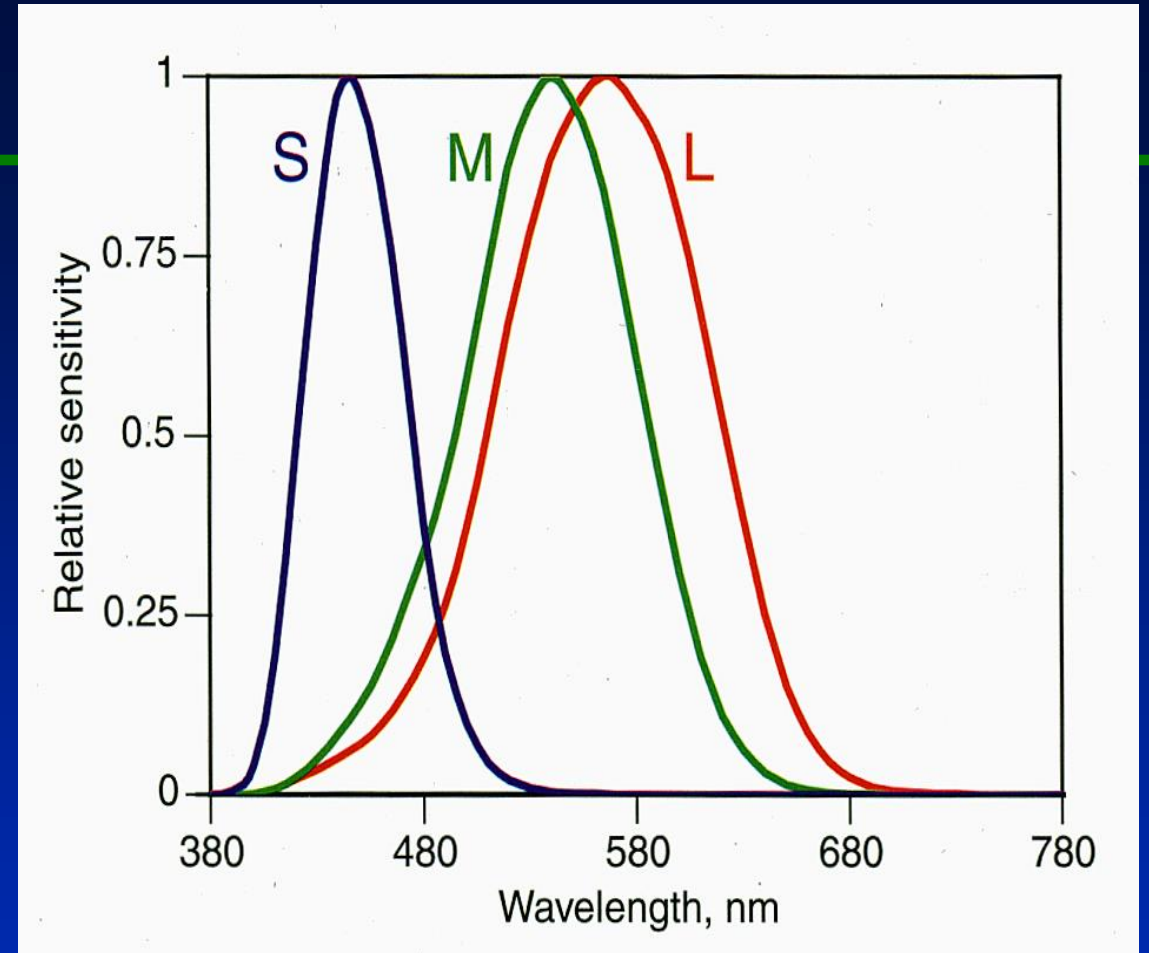


# Visible Light Spectrum



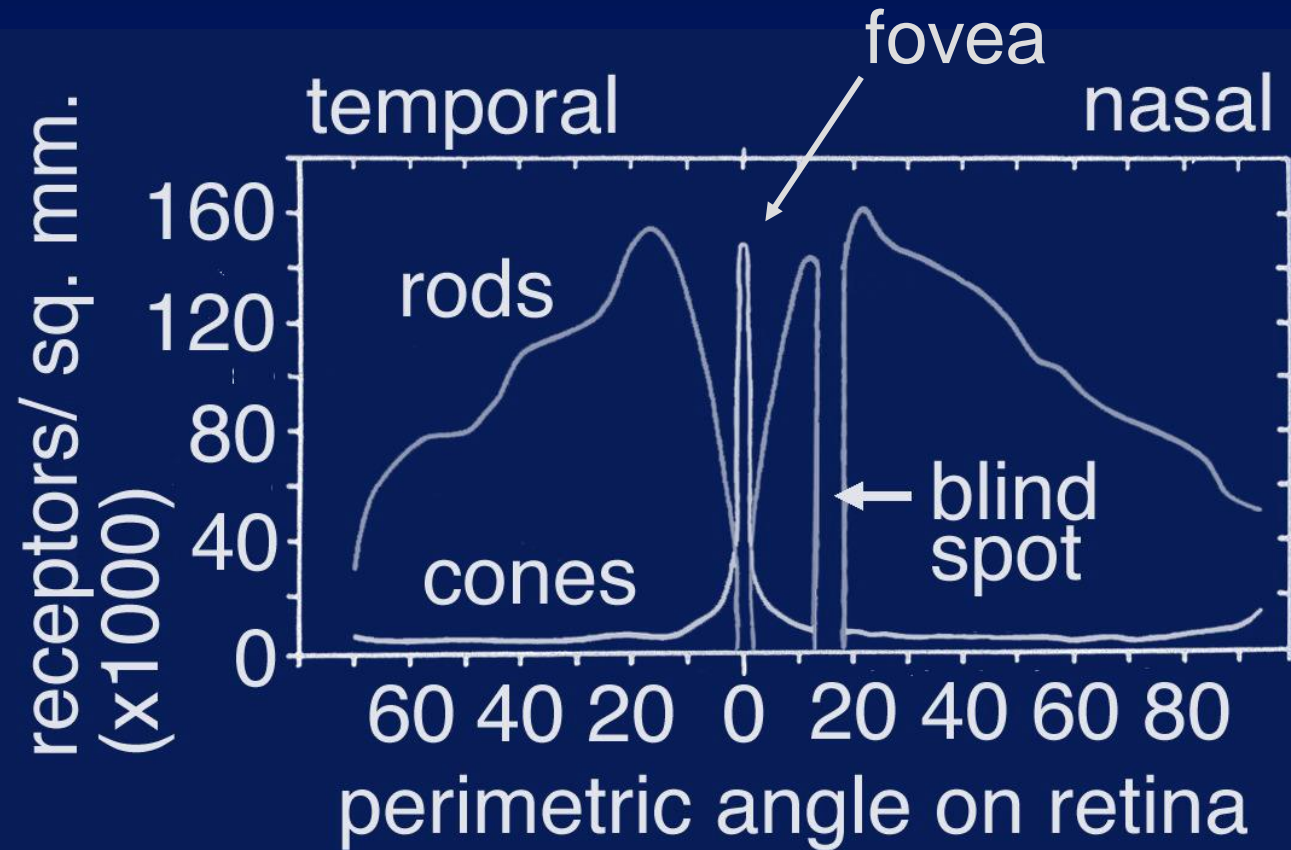
Dominant wavelengths of human receptor system  
The above are also frequently represented as BGR

## Relative Spectral Sensitivity (normalized)

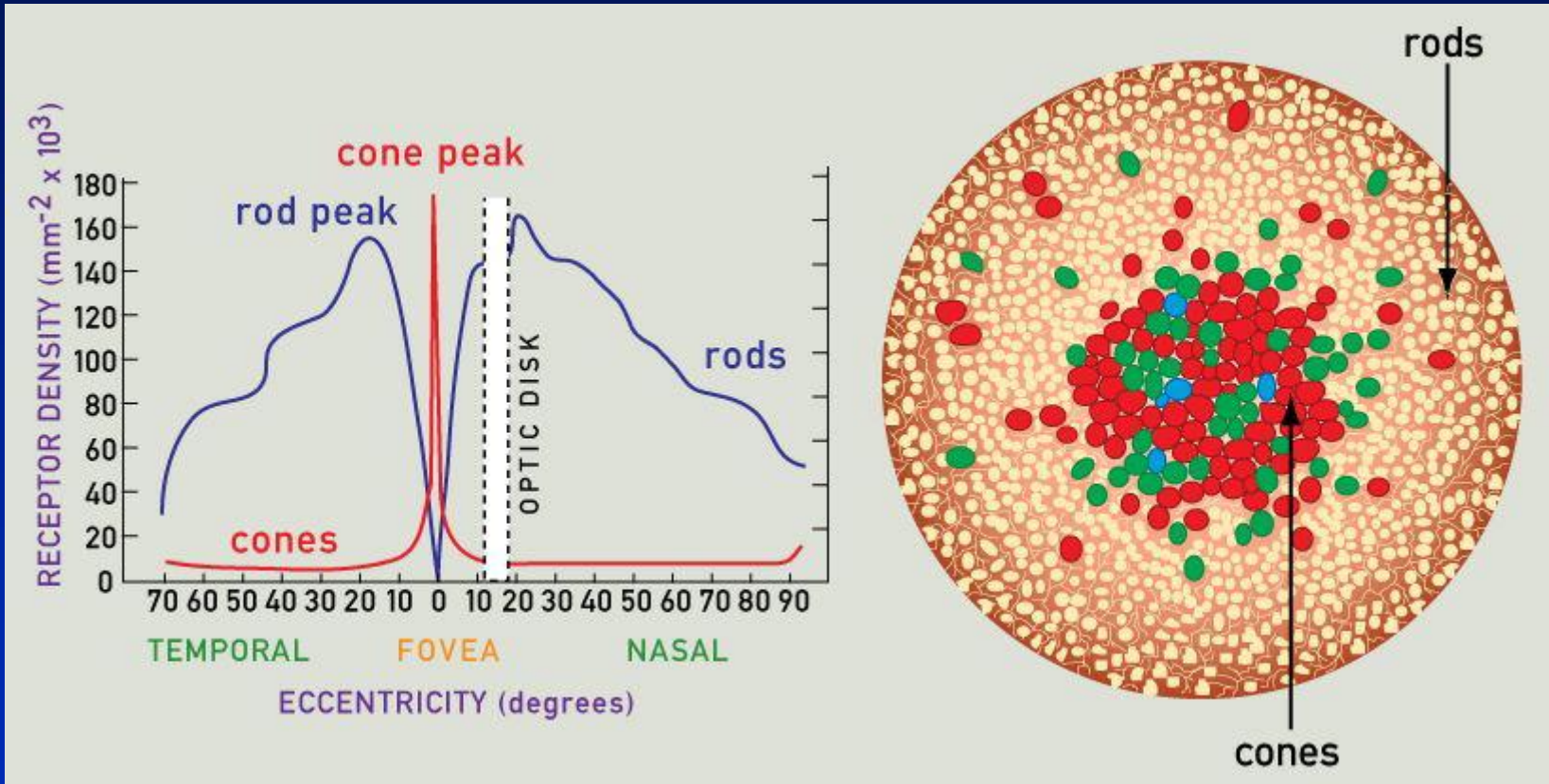


The relative spectral sensitivity of the L, M, and S cones (Stockman 1993). These spectral sensitivities are based on measurements in front of the eye rather than of isolated photoreceptors. Strictly speaking, these are called cone fundamentals.

# Receptor Distribution

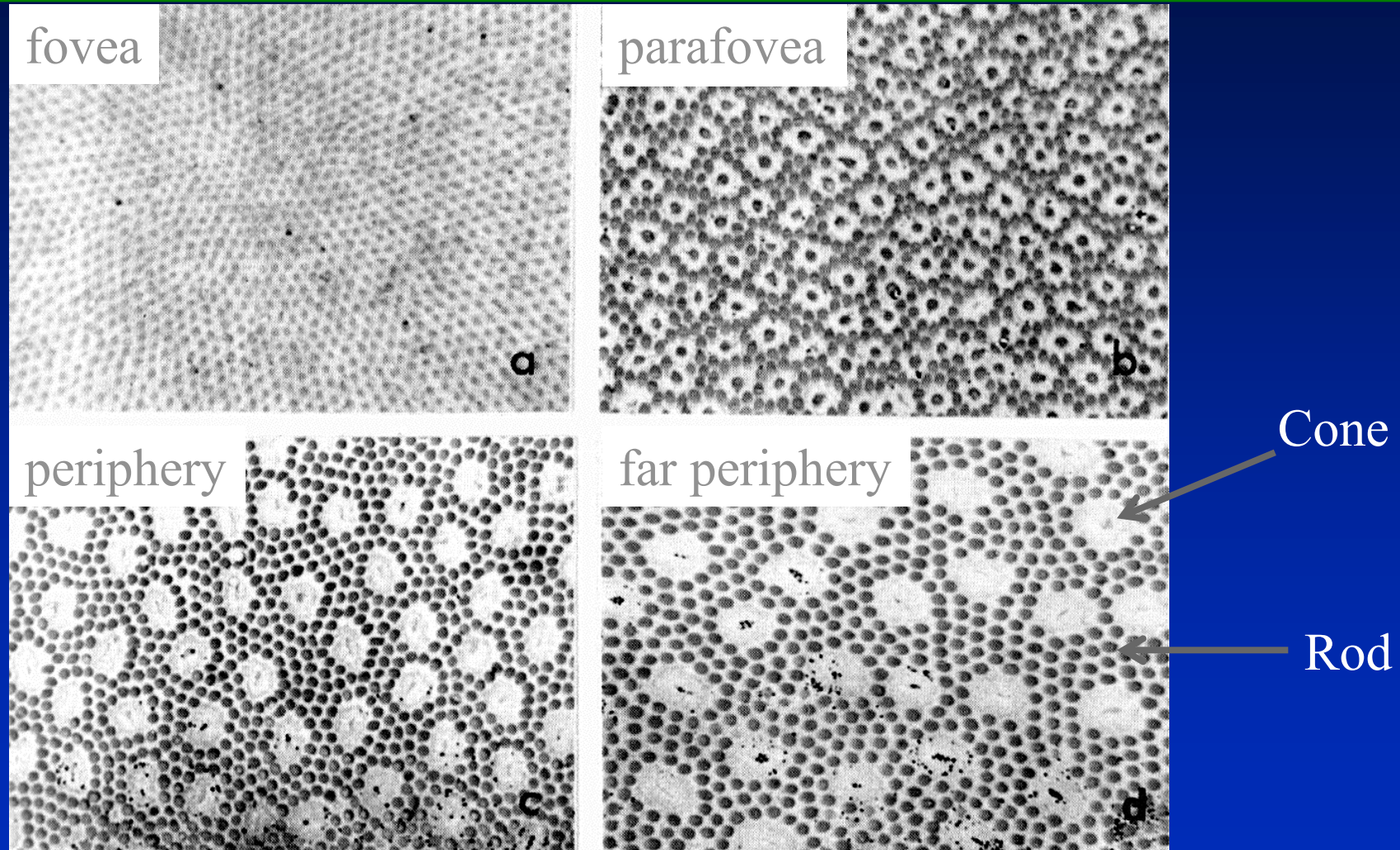


# Receptor Distribution





# Receptor Distribution



# Why RGB?

